



# **INTERFIS PROYECTOS EDUCATIVOS REPOSITORIO**

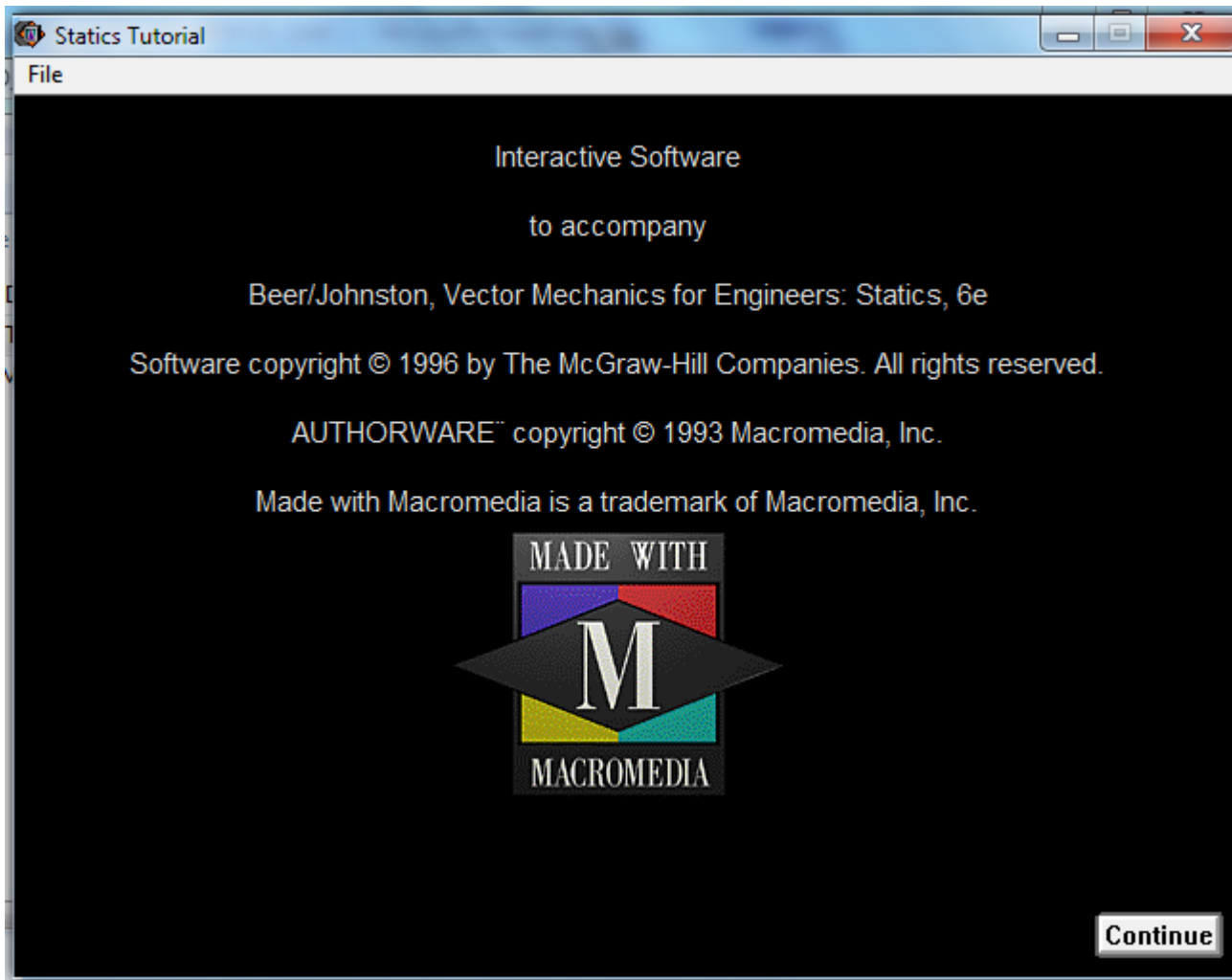
## **VIGA SIMPLEMENTE APOYADA**

**Ejercicios paso a paso a partir de Software STATICS**

**SHEAR & MOMENT DIAGRAMS.  
QUIZZES  
VIGA SIMPLEMENTE APOYADA  
(QUIZ 3 – 4 – 6 – 7)**

Los ejercicios siguientes se realizan con el **SOFTWARE STATICS**, incluido en “MECÁNICA VECTORIAL PARA INGENIEROS. ESTÁTICA”. Sexta edición. MCGRAW-HILL. 1997 ISBN 84-481-1079-X.

La presentación se realiza exclusivamente con fines educativos, para facilitar su discusión en clase.



Statics Tutorial

File

Interactive Software

to accompany

Beer/Johnston, Vector Mechanics for Engineers: Statics, 6e

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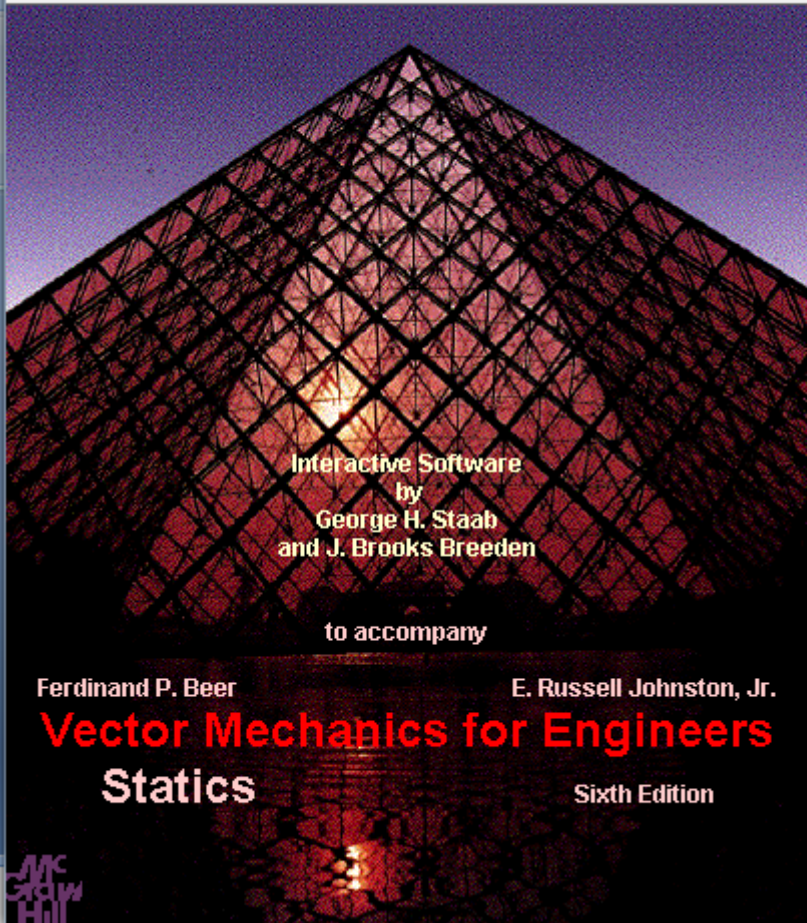


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Statics Tutorial

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Analysis of Structures

Beams and Friction

Quit

Statics Tutorial

File Shear & Moment Diagrams Friction

 Interactive Software  
by  
George H. Staab  
and J. Brooks Breeden

Ferdinand P. Beer

E. Russell Johnston, Jr.

# Vector Mechanics for Engineers

## Statics

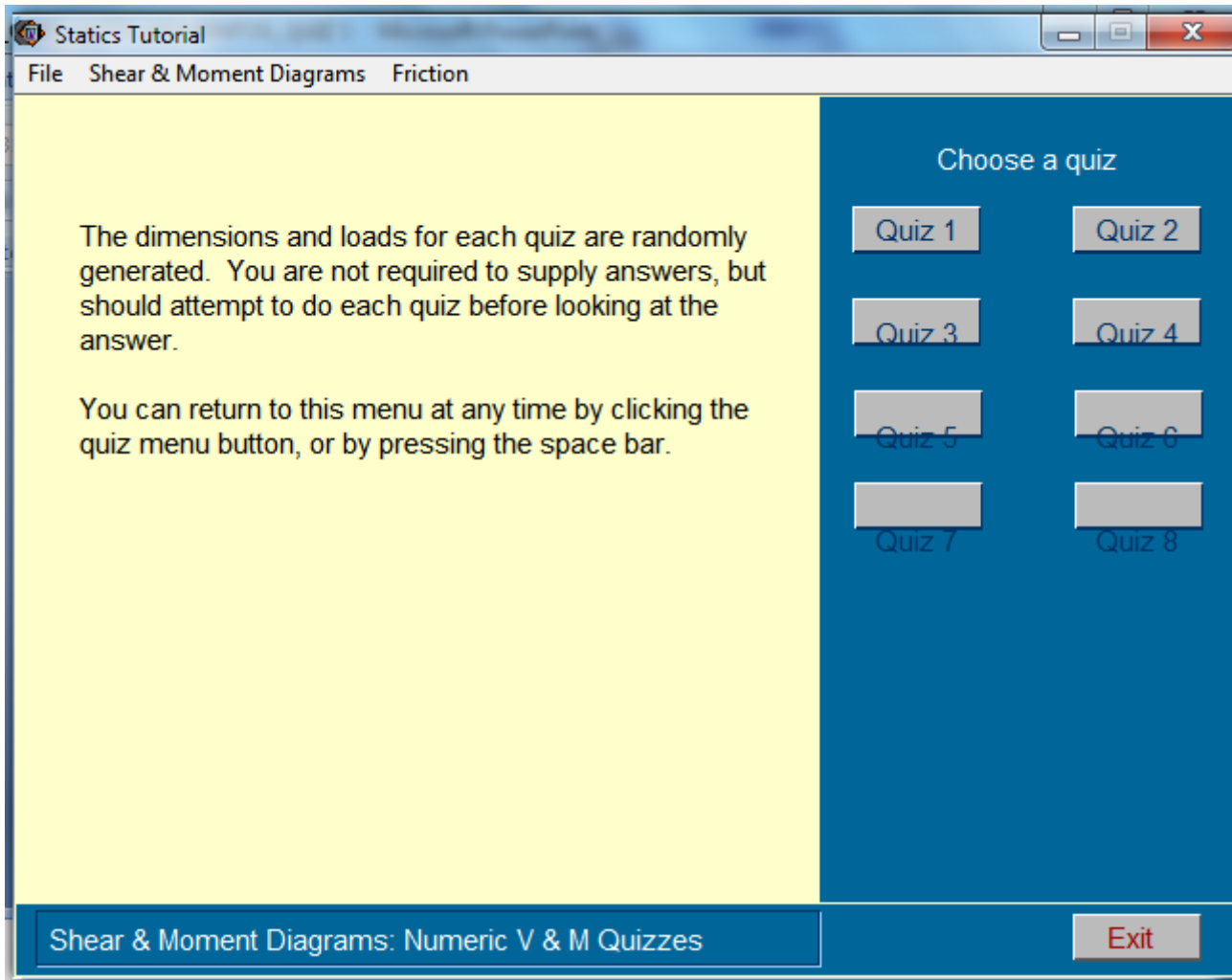
Sixth Edition

**Beams and Friction**  
The topics are as follows:

Shear & Moment Diagrams	(7.3-7.6)
Friction	(8.1-8.5)

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Statics Tutorial

File Shear & Moment Diagrams Friction

The dimensions and loads for each quiz are randomly generated. You are not required to supply answers, but should attempt to do each quiz before looking at the answer.

You can return to this menu at any time by clicking the quiz menu button, or by pressing the space bar.

Choose a quiz

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Quiz 5

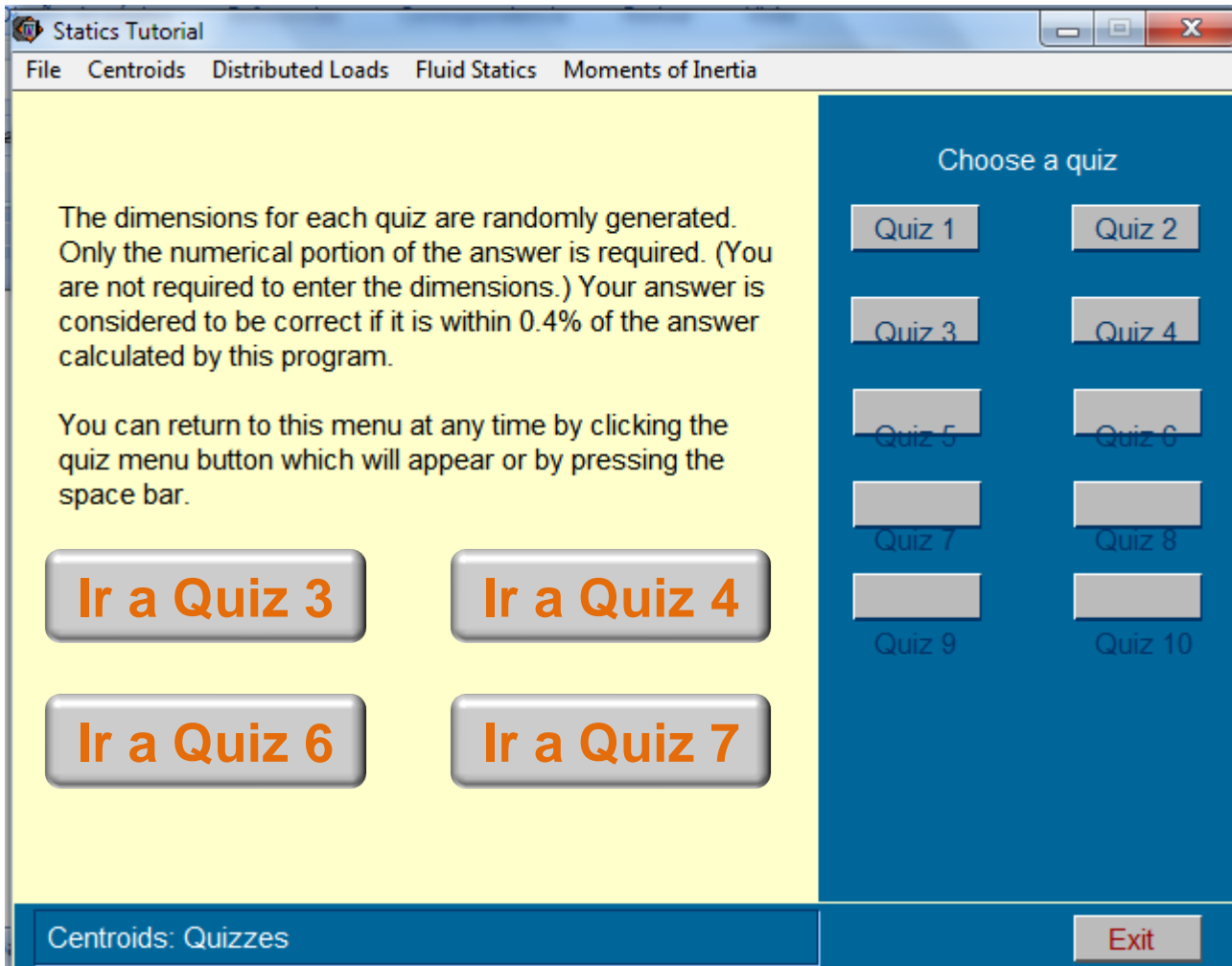
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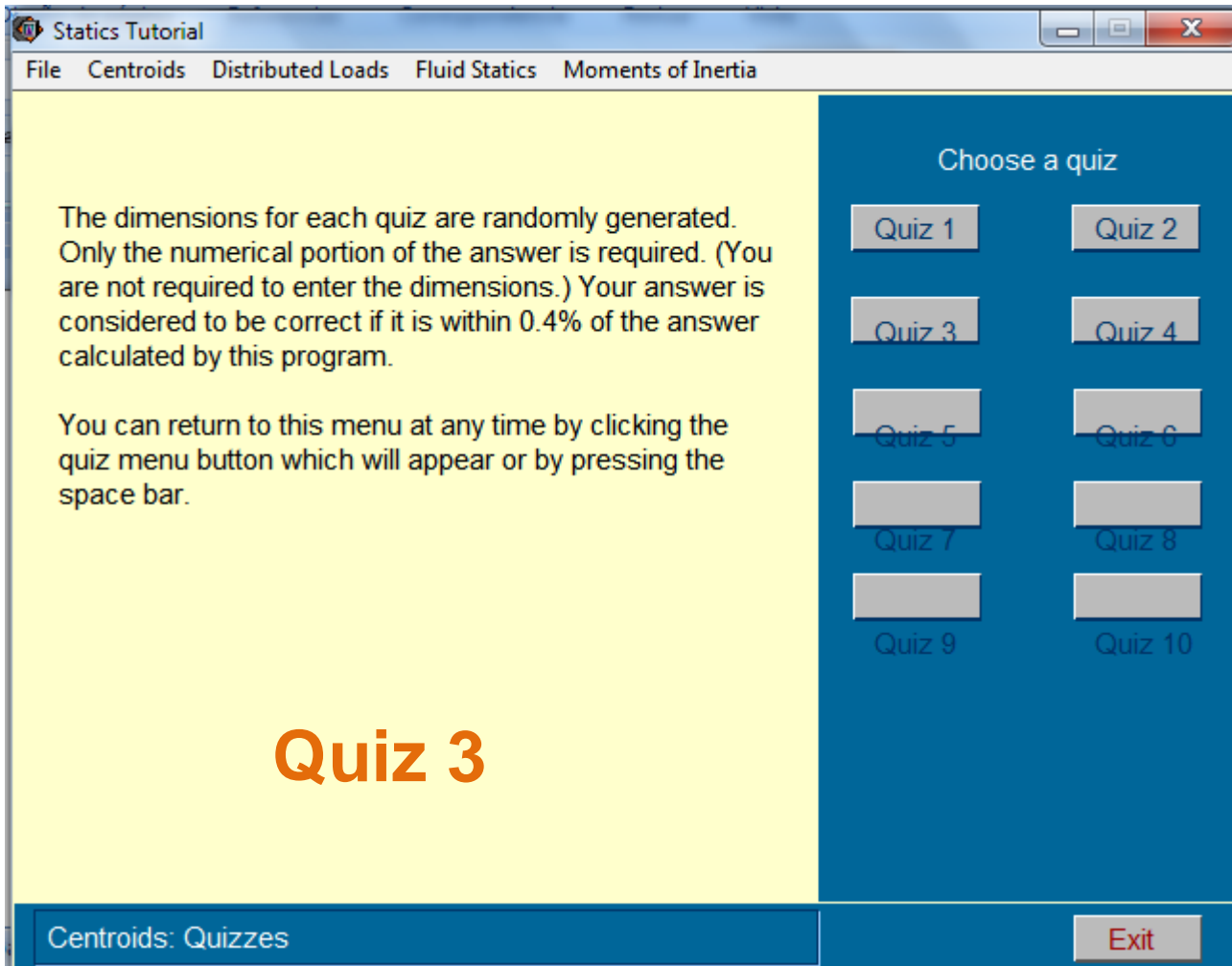
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Quiz 8

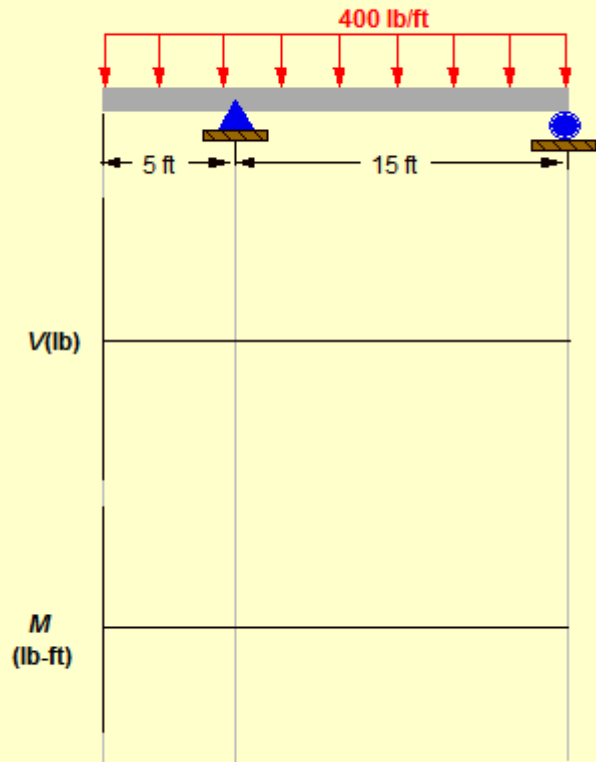
Shear & Moment Diagrams: Numeric V & M Quizzes

Exit





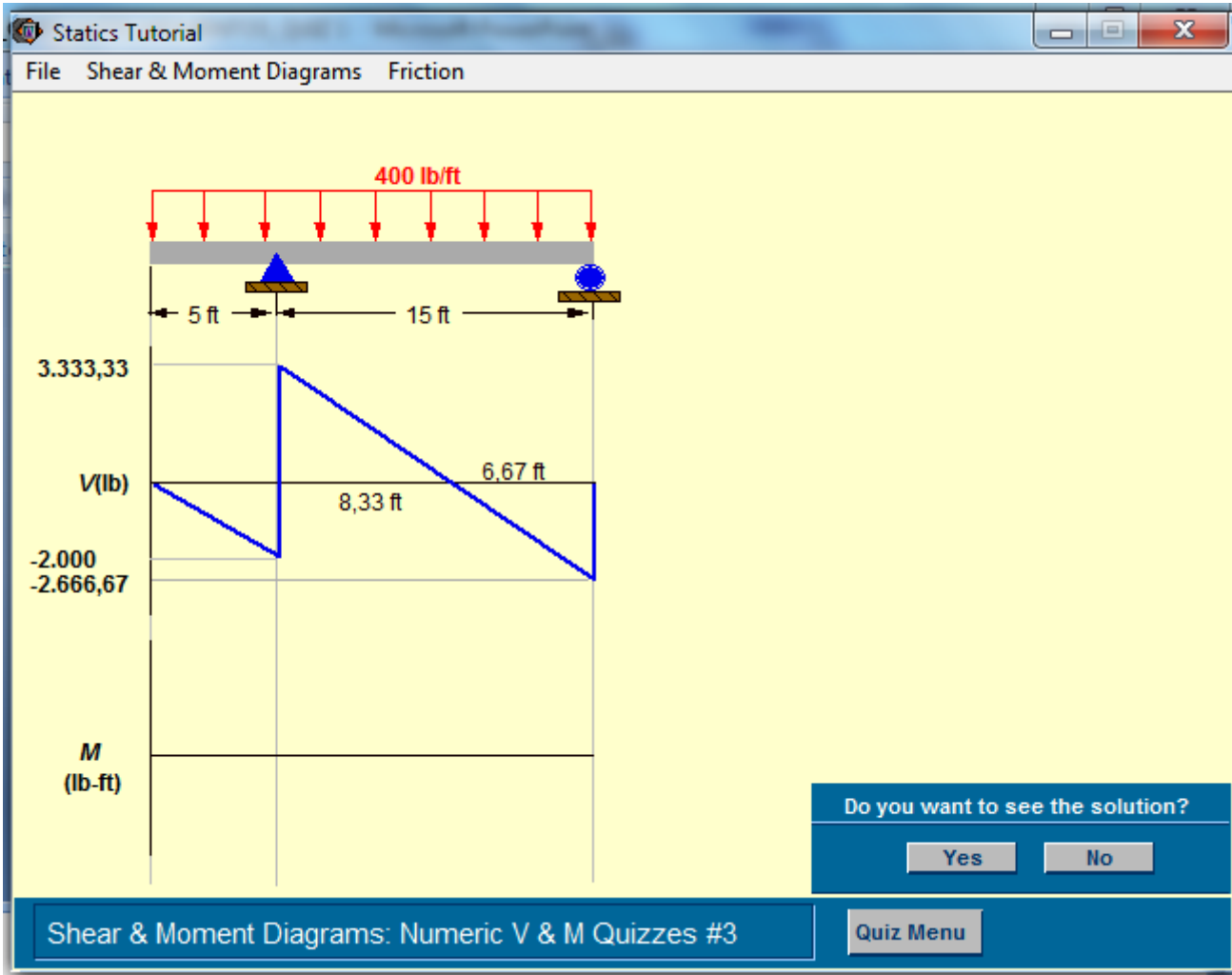


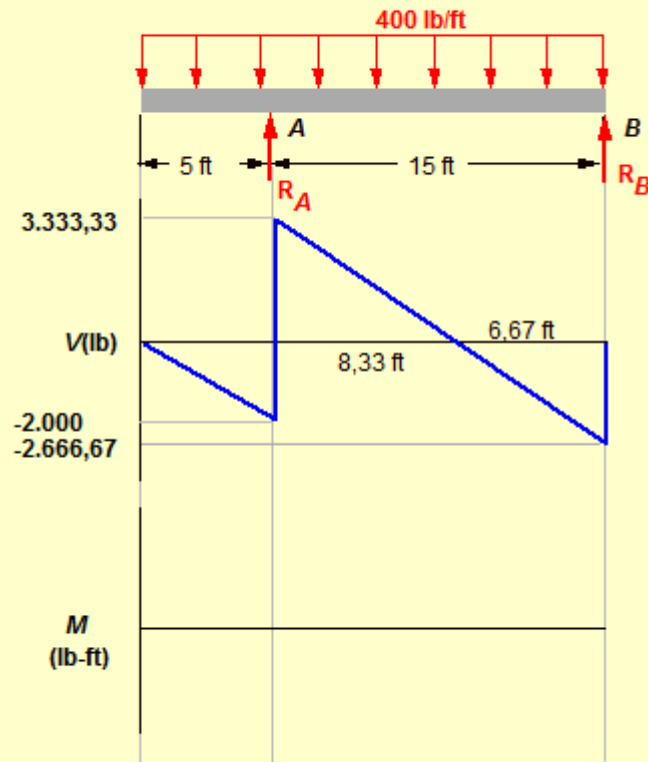


The simply supported beam shown is 20 ft long and supports a uniform load of 400 lb/ft over its span. Plot the shear and bending-moment diagrams. The horizontal reaction at **A** is zero.

After constructing your diagram, click the box below to see the correct shear diagram.

View Shear Force Diagram





First, establish the reactions at A and B. The reactions are determined by first modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions.

Statics Tutorial

File Shear & Moment Diagrams Friction

400(20) = 8.000 lb

5 ft

10 ft

5 ft

15 ft

A

B

$R_A$

$R_B$

3.333,33

V(lb)

8,33 ft

6,67 ft

-2.000

-2.666,67

M (lb-ft)

First, establish the reactions at A and B. The reactions are determined by first modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions of equilibrium are

$$+\uparrow \Sigma F_y = 0: R_A + R_B - 8.000 = 0$$

$$R_A + R_B = 8.000 \quad (1)$$

$$+\curvearrowleft \Sigma M_A = 0: 15(R_B) - 5(8.000) = 0$$

$$R_B = 2.666,67 \text{ lb}$$

Substituting 2.666,67 into equation (1) and solving yields  $R_A = 5.333,33 \text{ lb}$

Shear & Moment Diagrams: Numeric V & M Quizzes #3

Quiz Menu

Continue

Statics Tutorial

File Shear & Moment Diagrams Friction

400 lb/ft

5 ft 15 ft

A B

$R_A$   $R_B$

3.333,33

V(lb)

8,33 ft 6,67 ft

-2.000

-2.666,67

M (lb-ft)

First, establish the reactions at A and B. The reactions are determined by first modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions of equilibrium are

$$+\uparrow \Sigma F_y = 0: R_A + R_B - 8.000 = 0$$

$$R_A + R_B = 8.000 \quad (1)$$

$$+\curvearrowleft \Sigma M_A = 0: 15(R_B) - 5(8.000) = 0$$

$$R_B = 2.666,67 \text{ lb}$$

Substituting 2.666,67 into equation (1) and solving yields  $R_A = 5.333,33 \text{ lb}$

The shear diagram can be constructed once the reactions are known.

Shear & Moment Diagrams: Numeric V & M Quizzes #3

Quiz Menu

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Statics Tutorial

File Shear & Moment Diagrams Friction

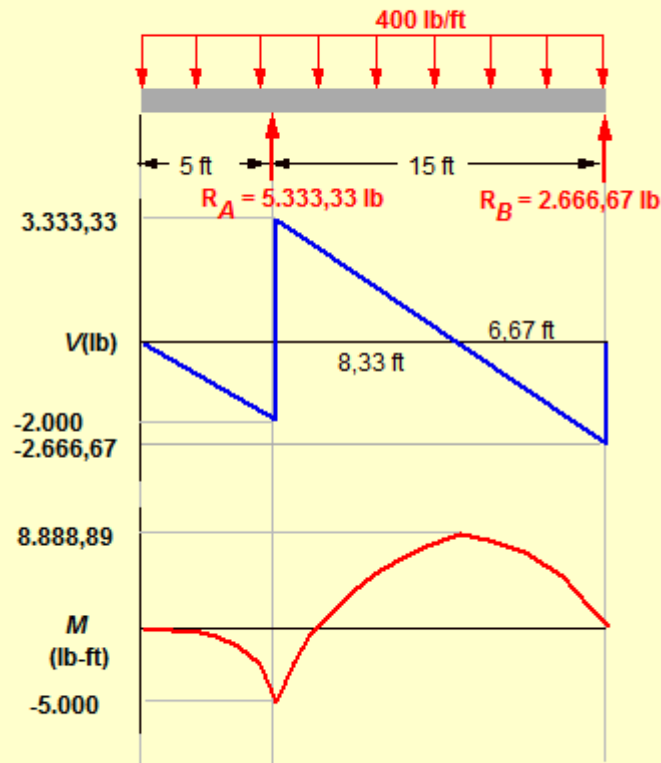
The diagram shows a beam of length 20 ft. A uniformly distributed load of 400 lb/ft is applied downwards. Reaction forces are  $R_A = 5.333,33 \text{ lb}$  at the left support and  $R_B = 2.666,67 \text{ lb}$  at the right support. The shear force diagram (V) starts at -2.000 lb at the left end, crosses the zero line at 5 ft, reaches a maximum of 3.333,33 lb at 8.33 ft, and ends at -2.666,67 lb at the right end. The moment diagram (M) starts at 0 lb-ft at the left end, reaches a maximum of 20.000 lb-ft at 8.33 ft, and ends at 0 lb-ft at the right end.

Click the button below to see the moment diagram.

View Moment Diagram

Shear & Moment Diagrams: Numeric V & M Quizzes #3

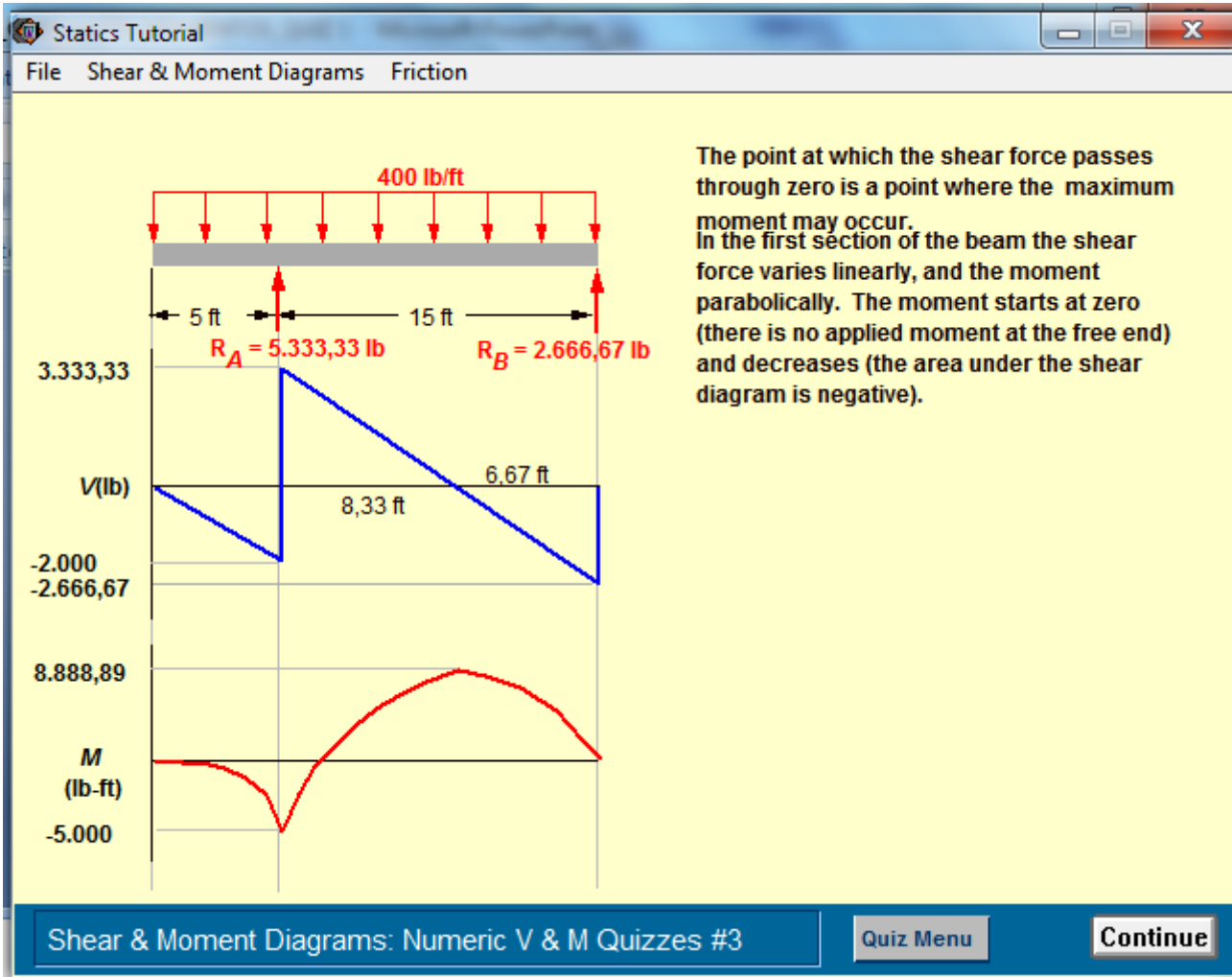
Quiz Menu



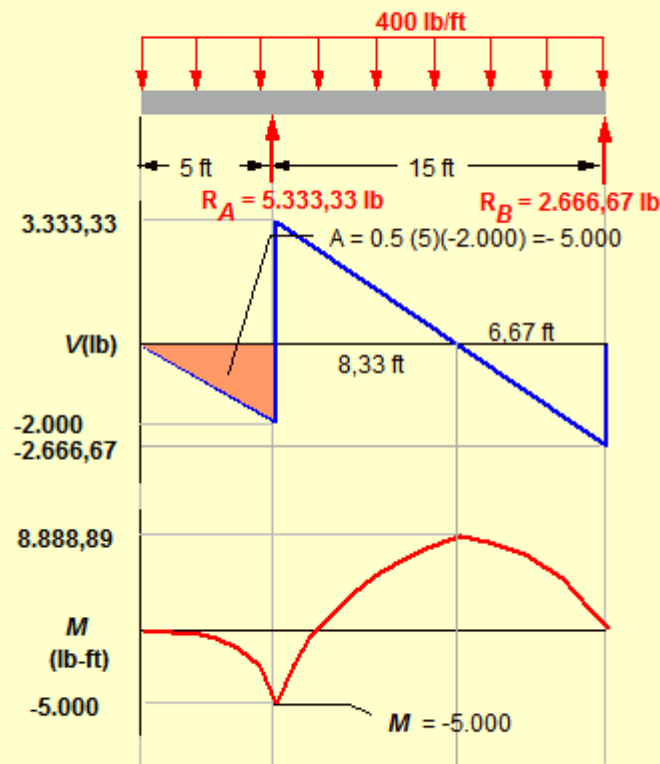
Do you want to see the solution?

Yes

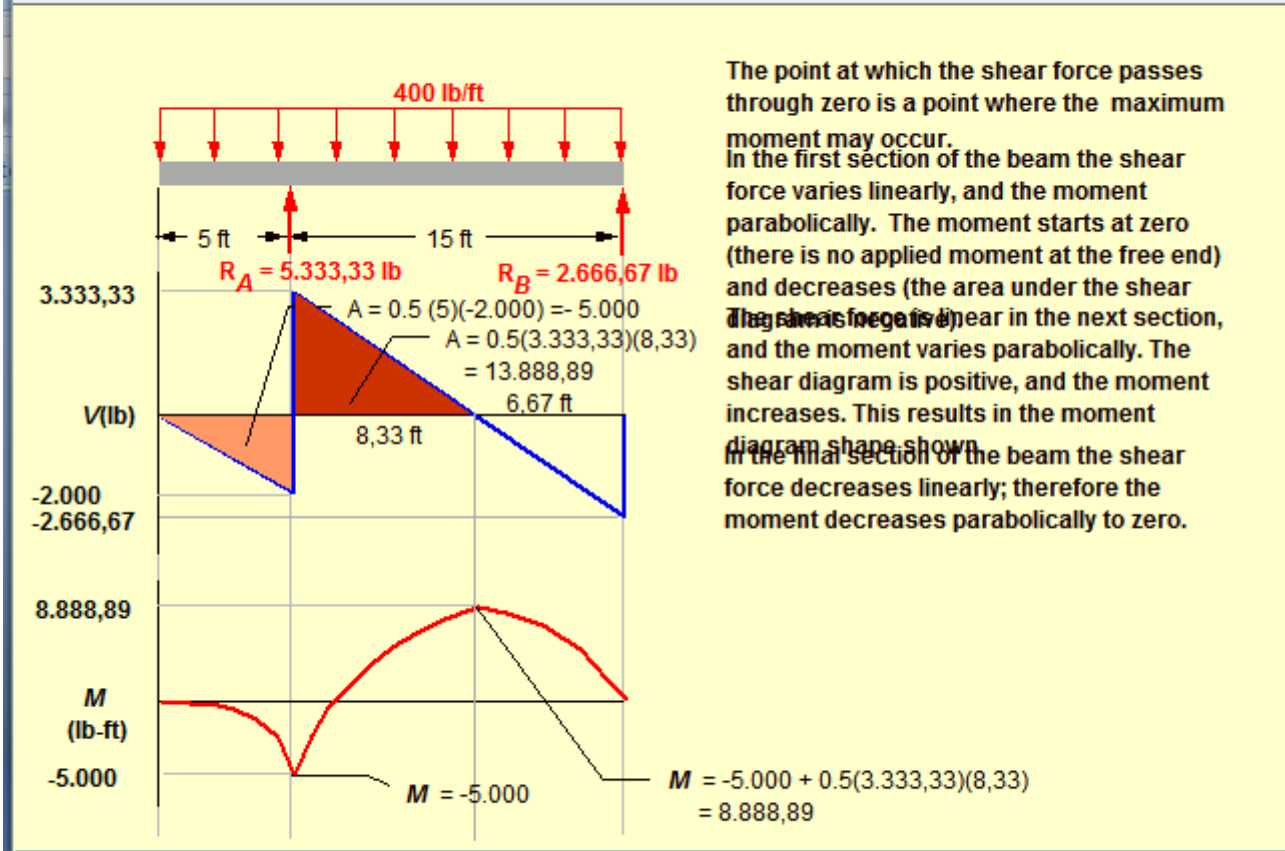
No



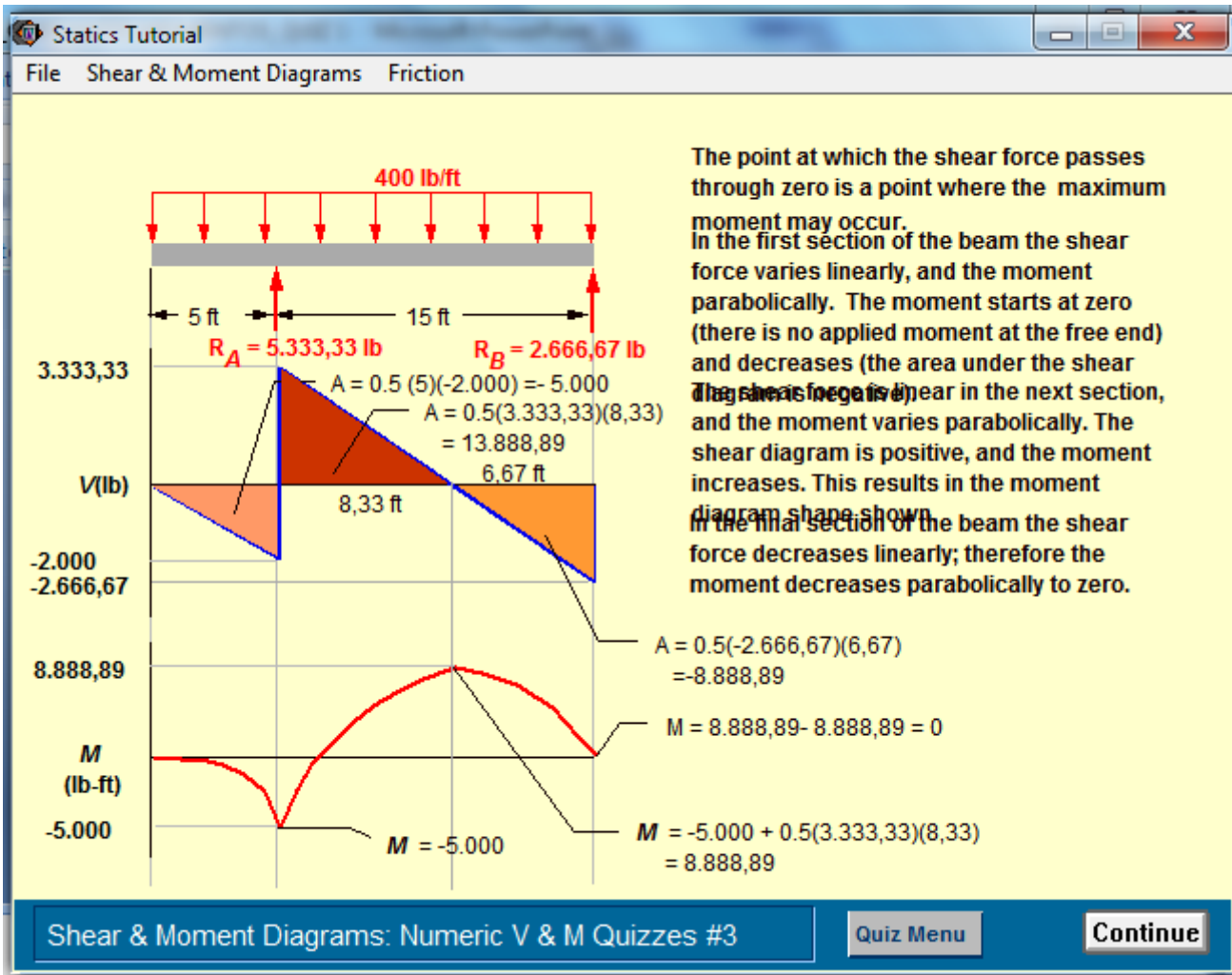


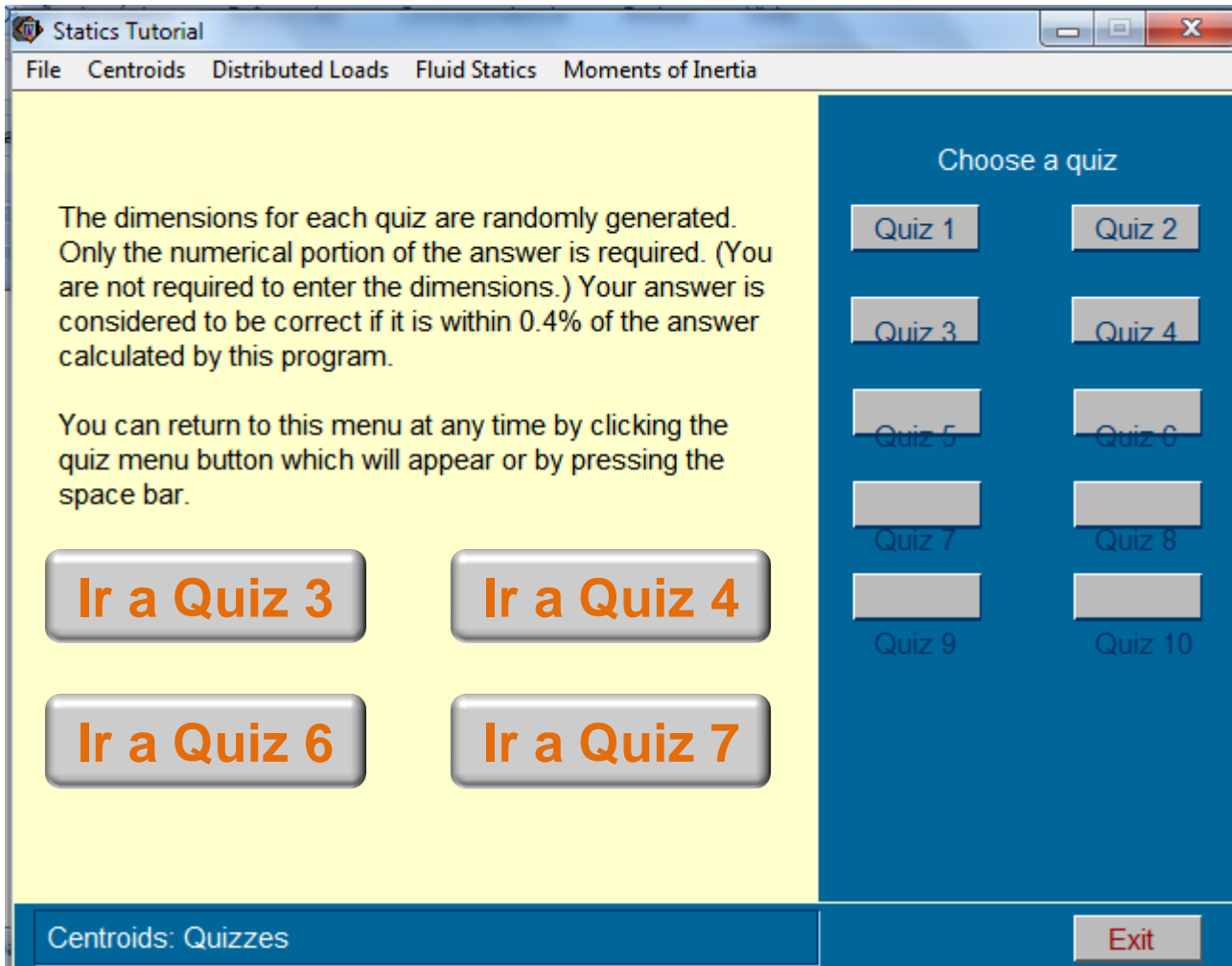


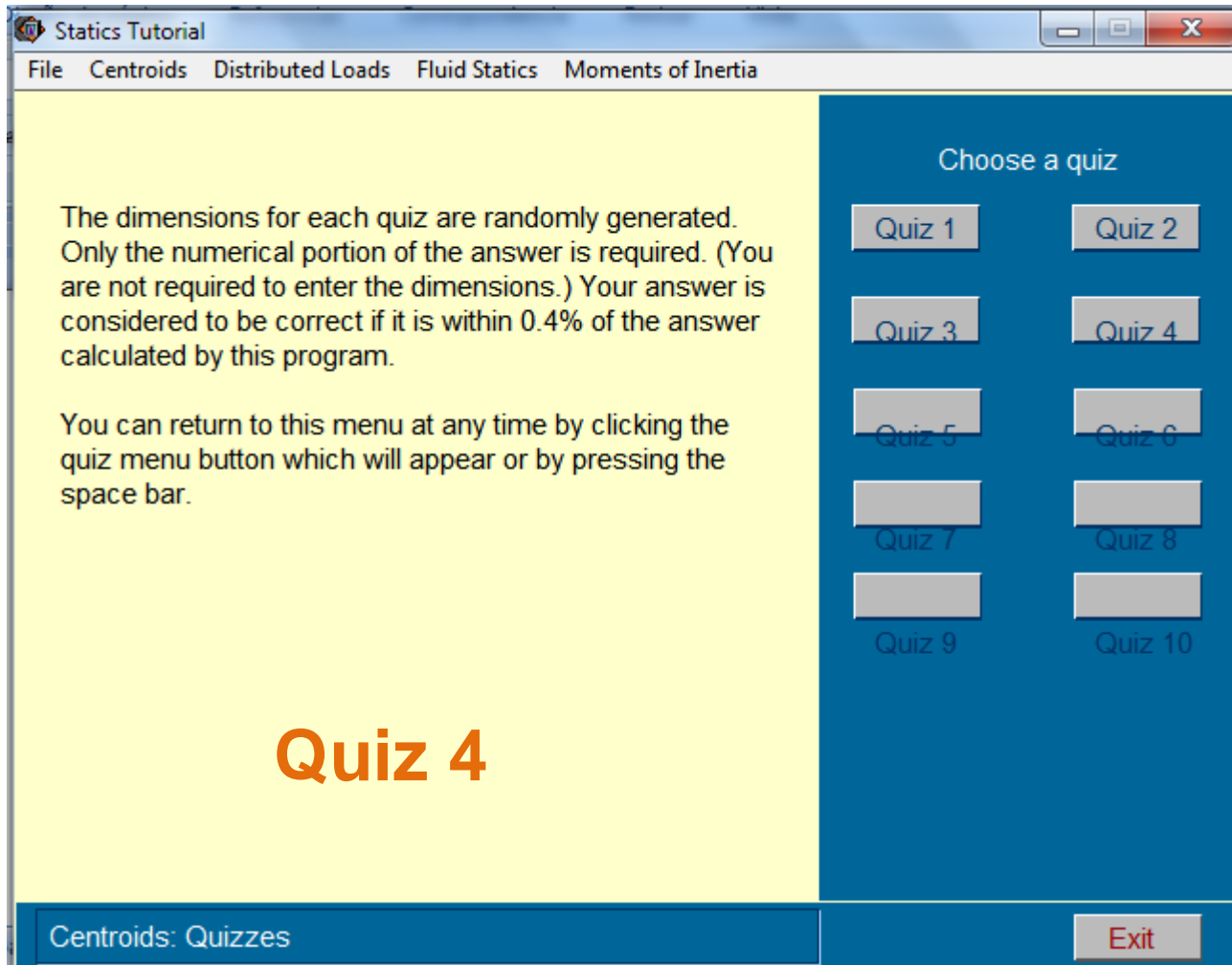
The point at which the shear force passes through zero is a point where the maximum moment may occur. In the first section of the beam the shear force varies linearly, and the moment varies parabolically. The moment starts at zero (there is no applied moment at the free end) and decreases (the area under the shear force is negative). The shear force is linear in the next section, and the moment varies parabolically. The shear diagram is positive, and the moment increases. This results in the moment diagram shape shown.

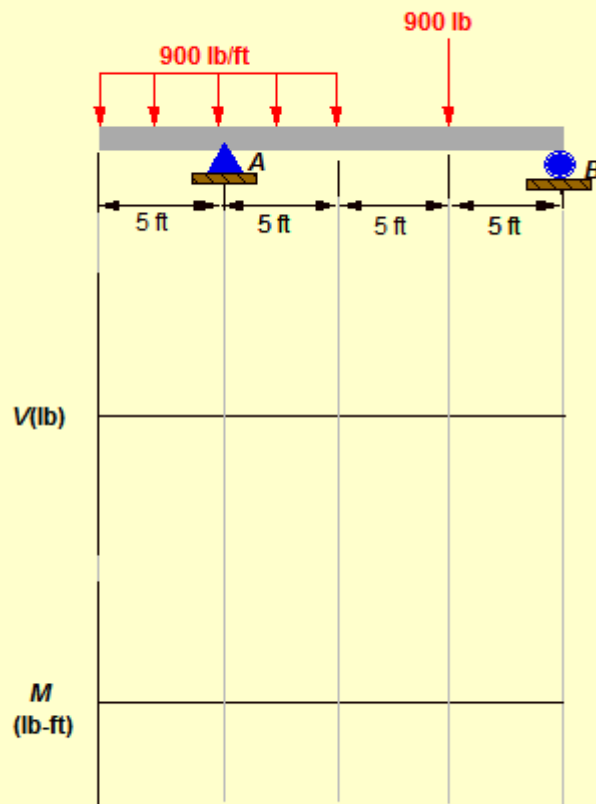


The point at which the shear force passes through zero is a point where the maximum moment may occur. In the first section of the beam the shear force varies linearly, and the moment varies parabolically. The moment starts at zero and decreases (the area under the shear force is negative). The shear force is linear in the next section, and the moment varies parabolically. The shear diagram is positive, and the moment increases. This results in the moment diagram shape shown. In the final section of the beam the shear force decreases linearly; therefore the moment decreases parabolically to zero.





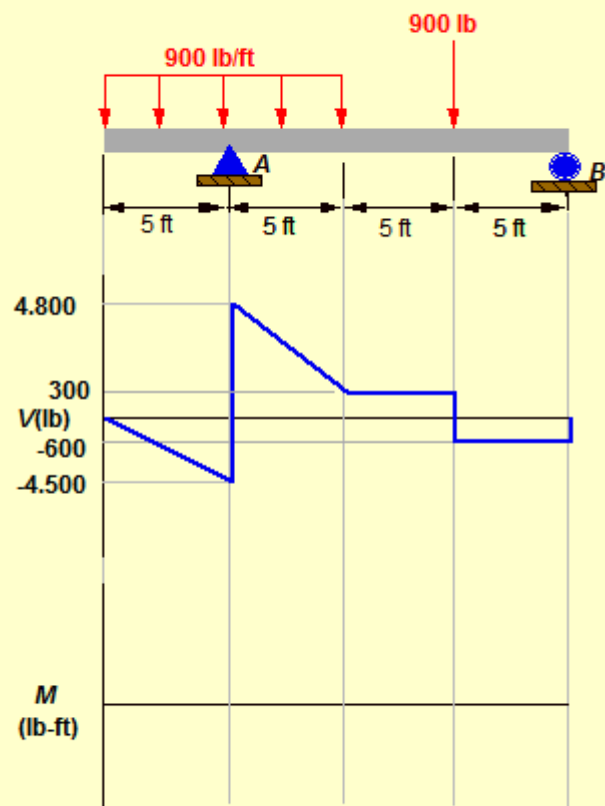




The 20-ft-long simply supported beam shown supports a uniform 900- lb/ft load over 10 ft of its span. A 900-lb concentrated load is applied 5 ft to the left of support **B**. Plot the shear and bending-moment diagrams for this beam. The horizontal reaction at **A** is zero.

After constructing your diagram, click the box below to see the correct shear diagram.

View Shear Force Diagram



Do you want to see the solution?

Yes

No

Statics Tutorial

File Shear & Moment Diagrams Friction

The diagram shows a beam of length 20 ft. A distributed load of 900 lb/ft is applied over the first 10 ft. A point load of 900 lb is applied at the 15 ft mark. Reaction forces  $R_A$  and  $R_B$  are shown at the supports. The Shear Force (V) diagram shows a linear decrease from 300 lb to -4500 lb over the first 5 ft, a jump to 4800 lb at the support, a linear decrease to 300 lb at 10 ft, a constant shear of 300 lb until 15 ft, a jump to -600 lb at the point load, and a constant shear of -600 lb until 20 ft. The Moment (M) diagram shows a parabolic curve from 0 to -4500 lb-ft at 5 ft, a linear increase to 4800 lb-ft at 10 ft, a constant moment of 4800 lb-ft until 15 ft, a linear decrease to -600 lb-ft at 20 ft.

900 lb/ft

900 lb

5 ft 5 ft 5 ft 5 ft

$R_A$   $R_B$

4.800

300

V(lb)

-600

-4.500

M (lb-ft)

First, establish the reactions at A and B.

The reactions are determined by modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions.

Shear & Moment Diagrams: Numeric V & M Quizzes #4

Quiz Menu

Continue



Statics Tutorial

File Shear & Moment Diagrams Friction

The diagram shows a horizontal beam of length 20 ft, divided into four 5 ft segments. A distributed load of 900 lb/ft is applied over the first 10 ft, with an equivalent concentrated load of 9,000 lb at the center (10 ft from the left). A point load of 900 lb is applied at the 15 ft mark. Reaction forces  $R_A$  and  $R_B$  are shown at the left and right ends, respectively. The Shear Force (V) diagram shows a linear decrease from 0 to -4,500 lb at 5 ft, a jump to 4,800 lb at 10 ft, a linear decrease to 300 lb at 15 ft, a jump to -600 lb at 15 ft, and a constant value of -600 lb until 20 ft. The Moment (M) diagram shows a parabolic curve from 0 to -4,500 lb-ft at 5 ft, a linear increase to 300 lb-ft at 10 ft, a constant value of 300 lb-ft until 15 ft, a jump to -600 lb-ft at 15 ft, and a constant value of -600 lb-ft until 20 ft.

900(10) = 9,000 lb

900 lb

5 ft

5 ft

5 ft

5 ft

A

B

$R_A$

$R_B$

4,800

300

V (lb)

-600

-4,500

M (lb-ft)

First, establish the reactions at A and B.

The reactions are determined by modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions.

The equations of equilibrium are

$+\uparrow \Sigma F_y = 0: R_A + R_B - 9,000 - 900 = 0$   
 $R_A + R_B = 9,900 \quad (1)$

$+\curvearrowleft \Sigma M_A = 0: 15(R_B) - 10(900) = 0$   
 $R_B = 600 \text{ lb}$

Substituting 600 lb into equation (1) and solving yields  
 $R_A = 9,300 \text{ lb}$

Shear & Moment Diagrams: Numeric V & M Quizzes #4

Quiz Menu

Continue

Statics Tutorial

File Shear & Moment Diagrams Friction

900 lb/ft

900 lb

A

B

5 ft 5 ft 5 ft 5 ft

4.800

300

V (lb)

-600

-4.500

M (lb-ft)

First, establish the reactions at A and B.

The reactions are determined by modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions.

The equations of equilibrium are

$$+\uparrow \Sigma F_y = 0: R_A + R_B - 9.000 - 900 = 0$$

$$R_A + R_B = 9.900 \quad (1)$$

$$+\curvearrowleft \Sigma M_A = 0: 15(R_B) - 10(900) = 0$$

$$R_B = 600 \text{ lb}$$

Substituting 600 lb into equation (1) and solving yields

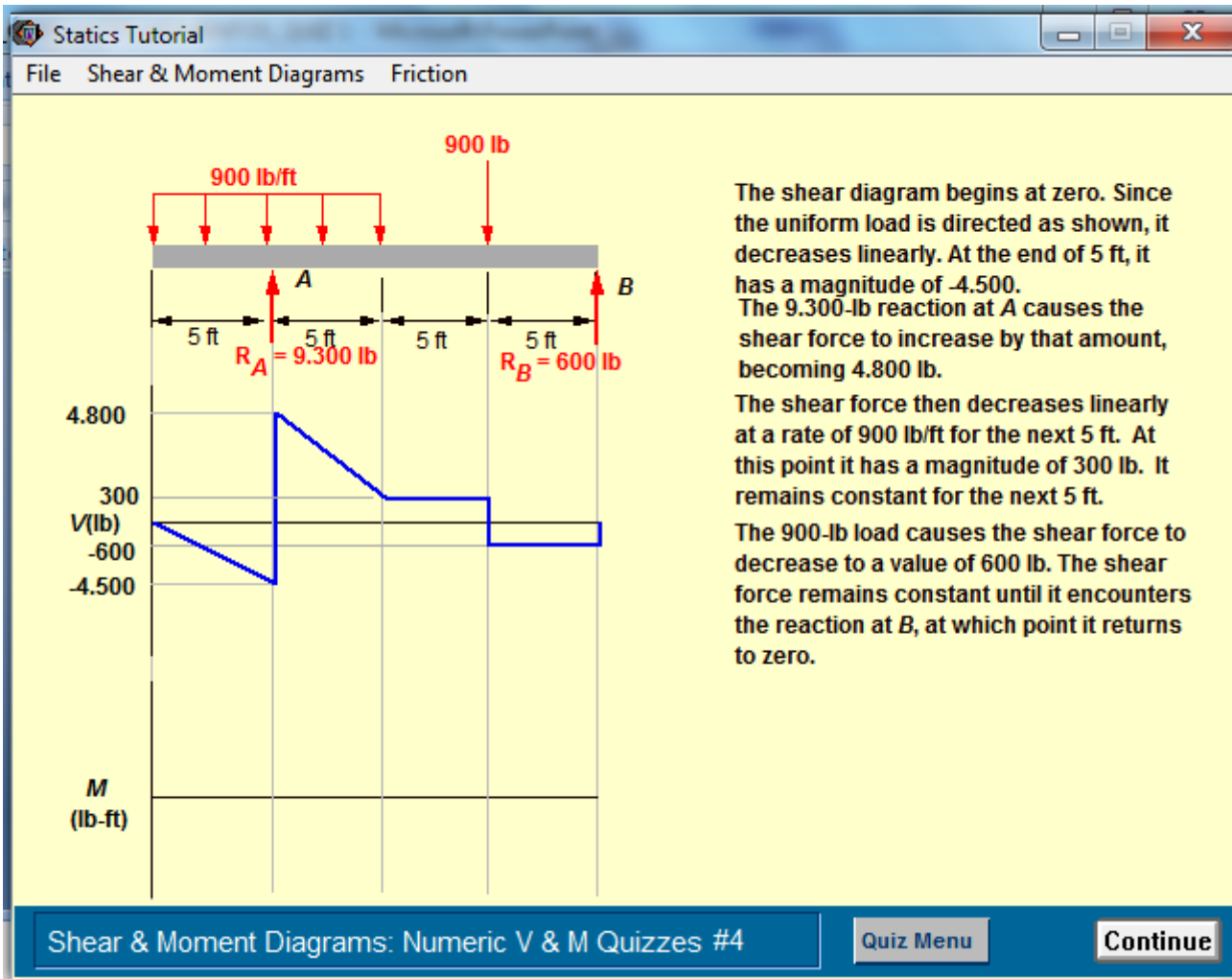
$$R_A = 9.300 \text{ lb}$$

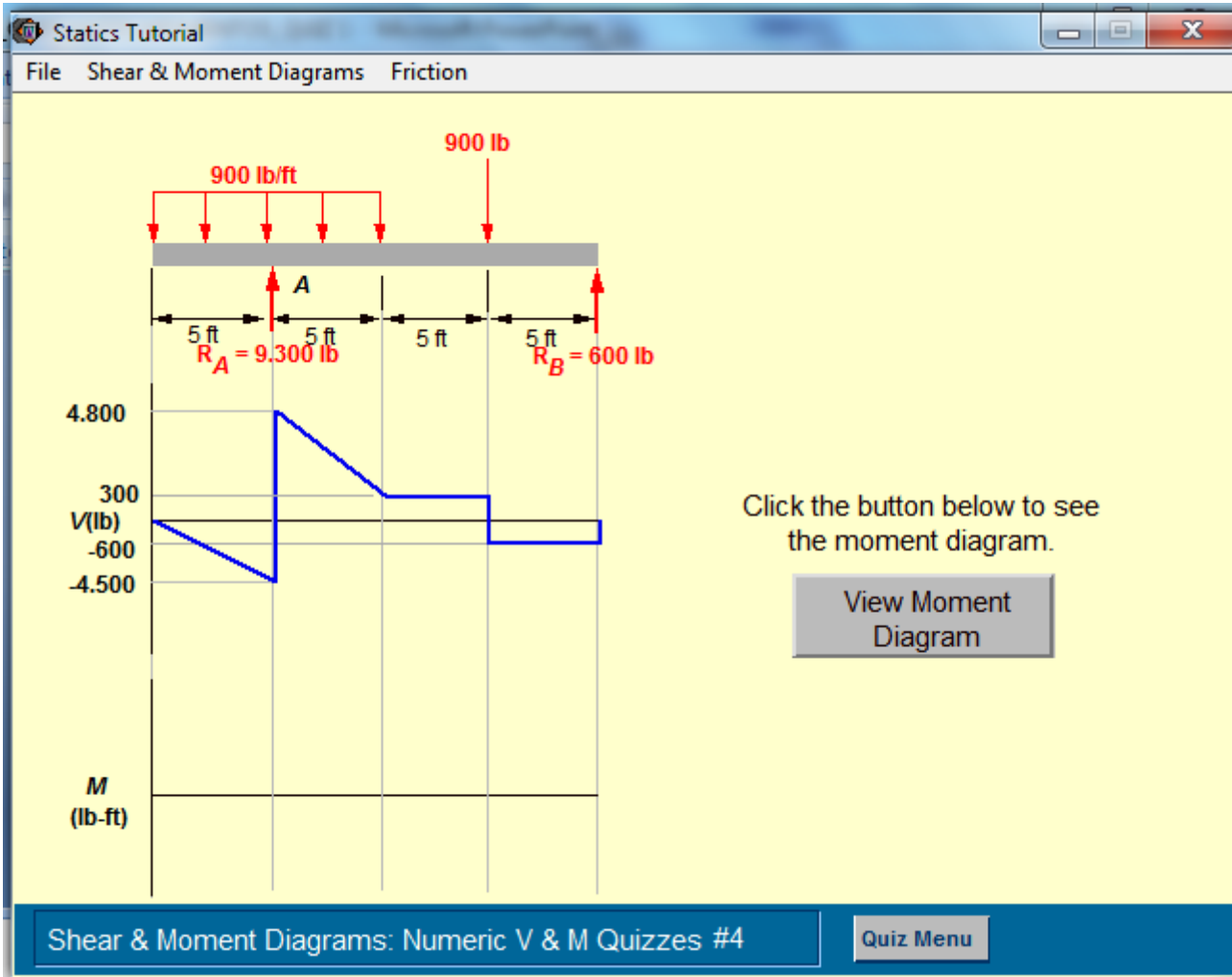
The shear diagram can be constructed once the reactions are known.

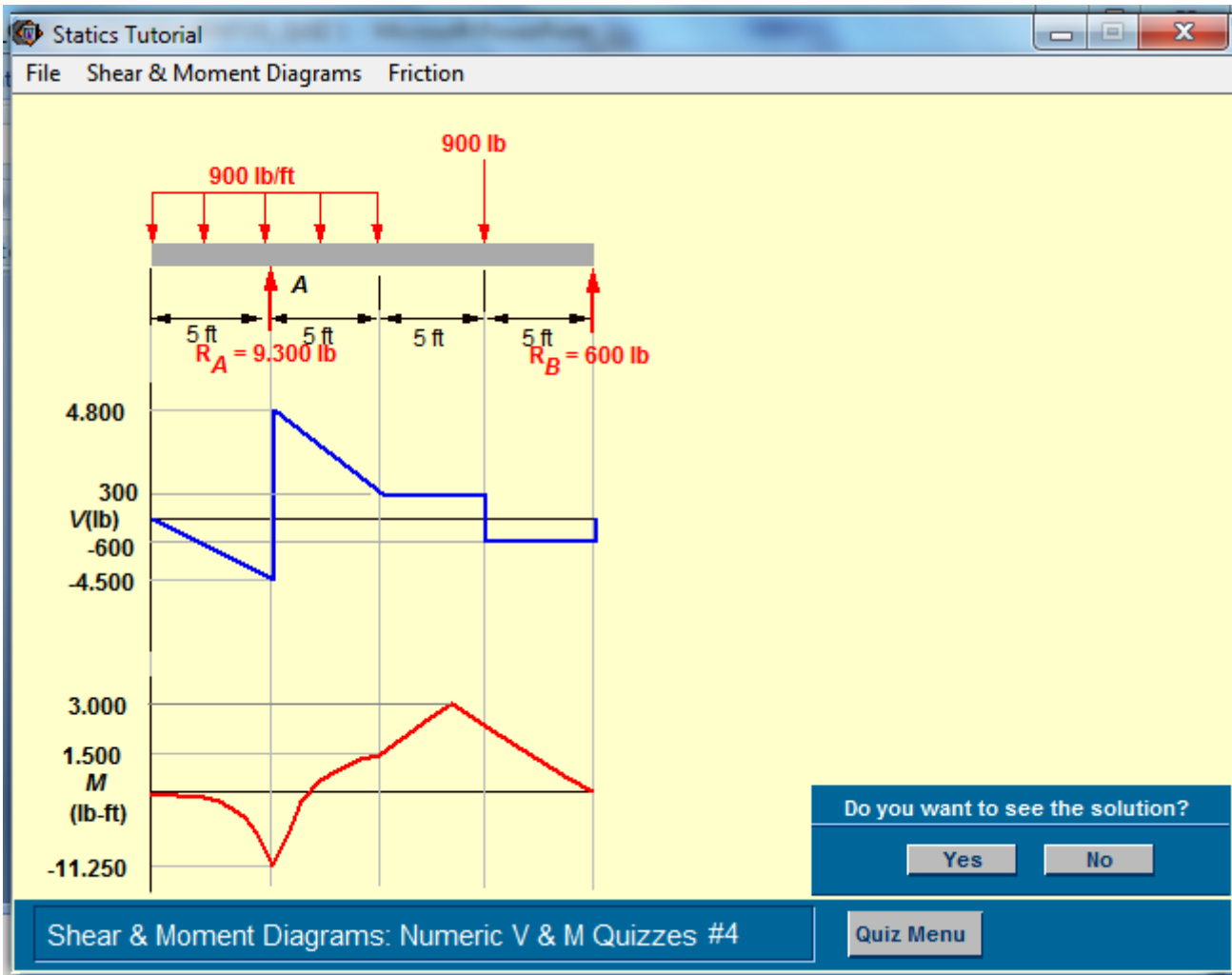
Shear & Moment Diagrams: Numeric V & M Quizzes #4

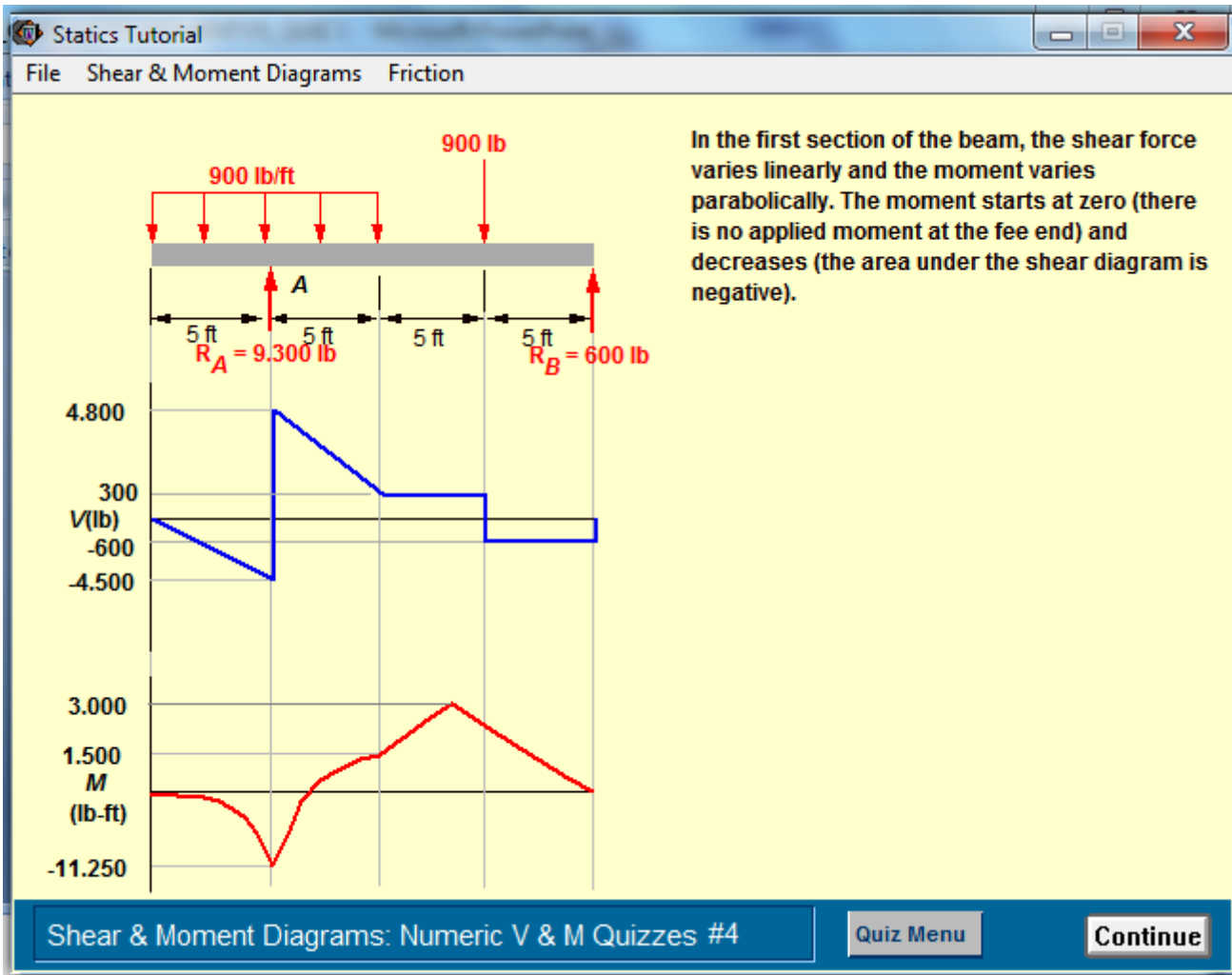
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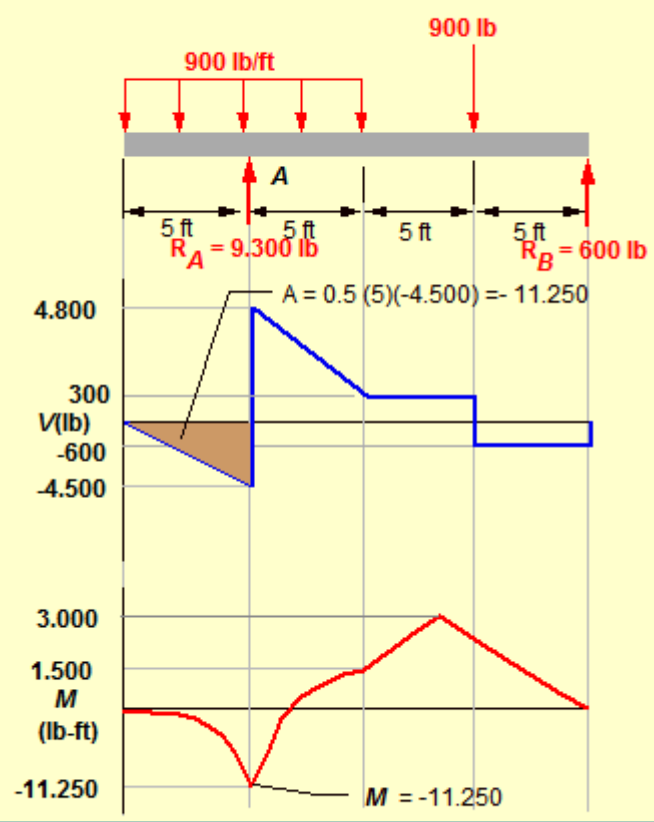
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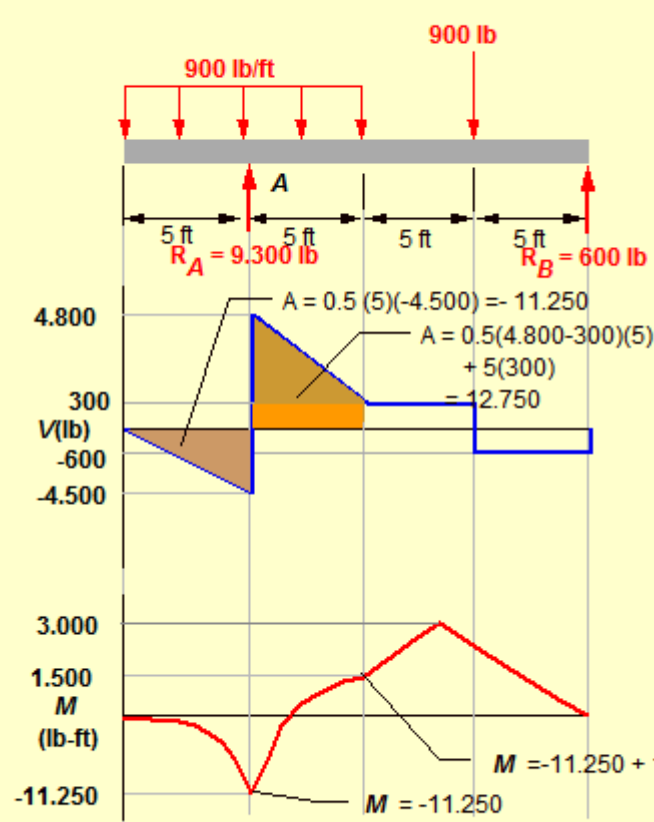








In the first section of the beam, the shear force varies linearly and the moment varies parabolically. The moment starts at zero (there is no applied moment at the free end) and decreases (the area under the shear diagram is negative). In the next section, the shear force is linear and the moment varies parabolically. The shear diagram is positive, and the moment increases. This results in the moment diagram shape shown. Finding the area under the shear diagram in this section of the beam requires computing two areas.

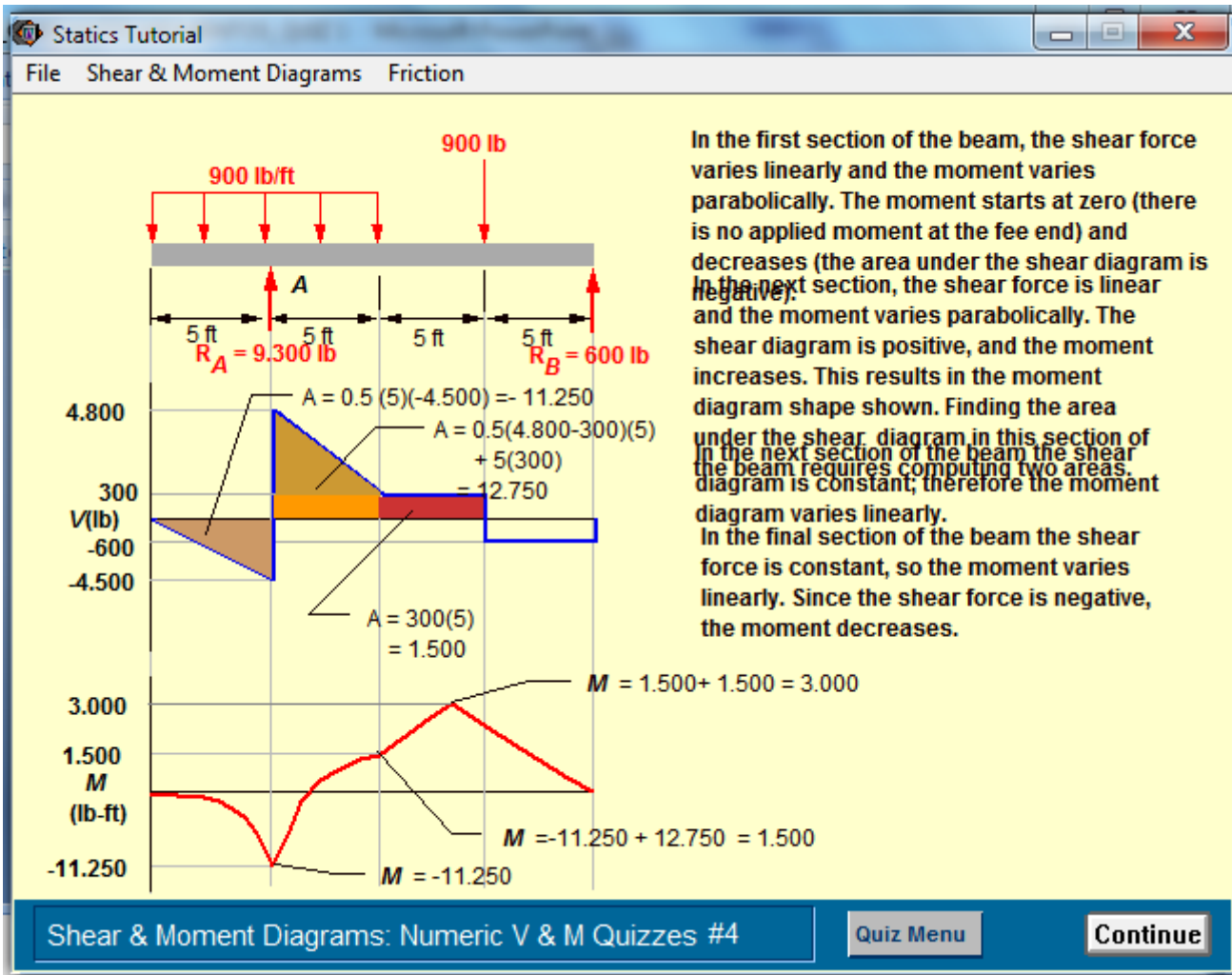


In the first section of the beam, the shear force varies linearly and the moment varies parabolically. The moment starts at zero (there is no applied moment at the free end) and decreases (the area under the shear diagram is negative).

In the next section, the shear force is linear and the moment varies parabolically. The shear diagram is positive, and the moment increases. This results in the moment diagram shape shown. Finding the area under the shear diagram in this section of the beam requires computing two areas.

In the next section of the beam the shear diagram is constant; therefore the moment diagram varies linearly.



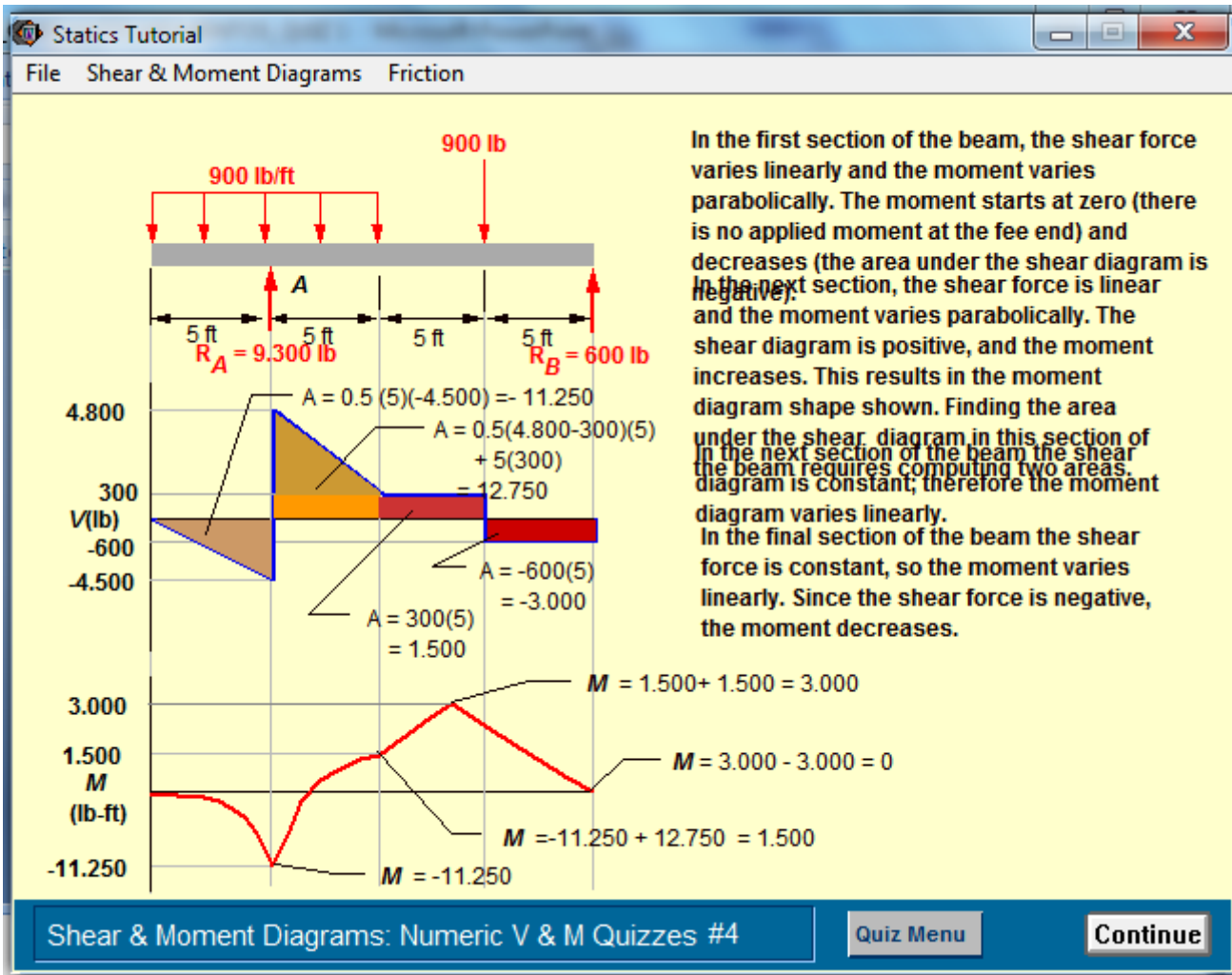


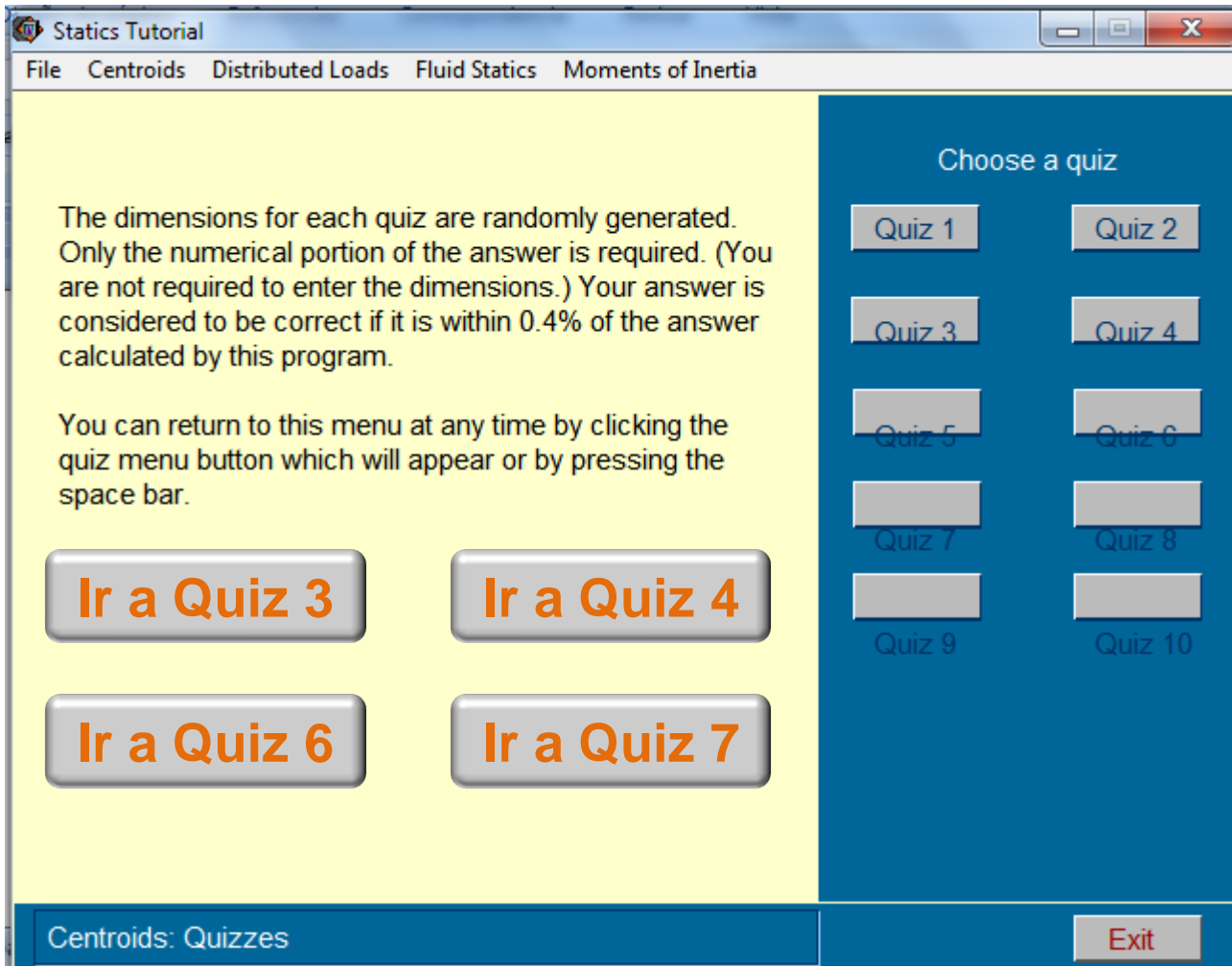
In the first section of the beam, the shear force varies linearly and the moment varies parabolically. The moment starts at zero (there is no applied moment at the free end) and decreases (the area under the shear diagram is negative).

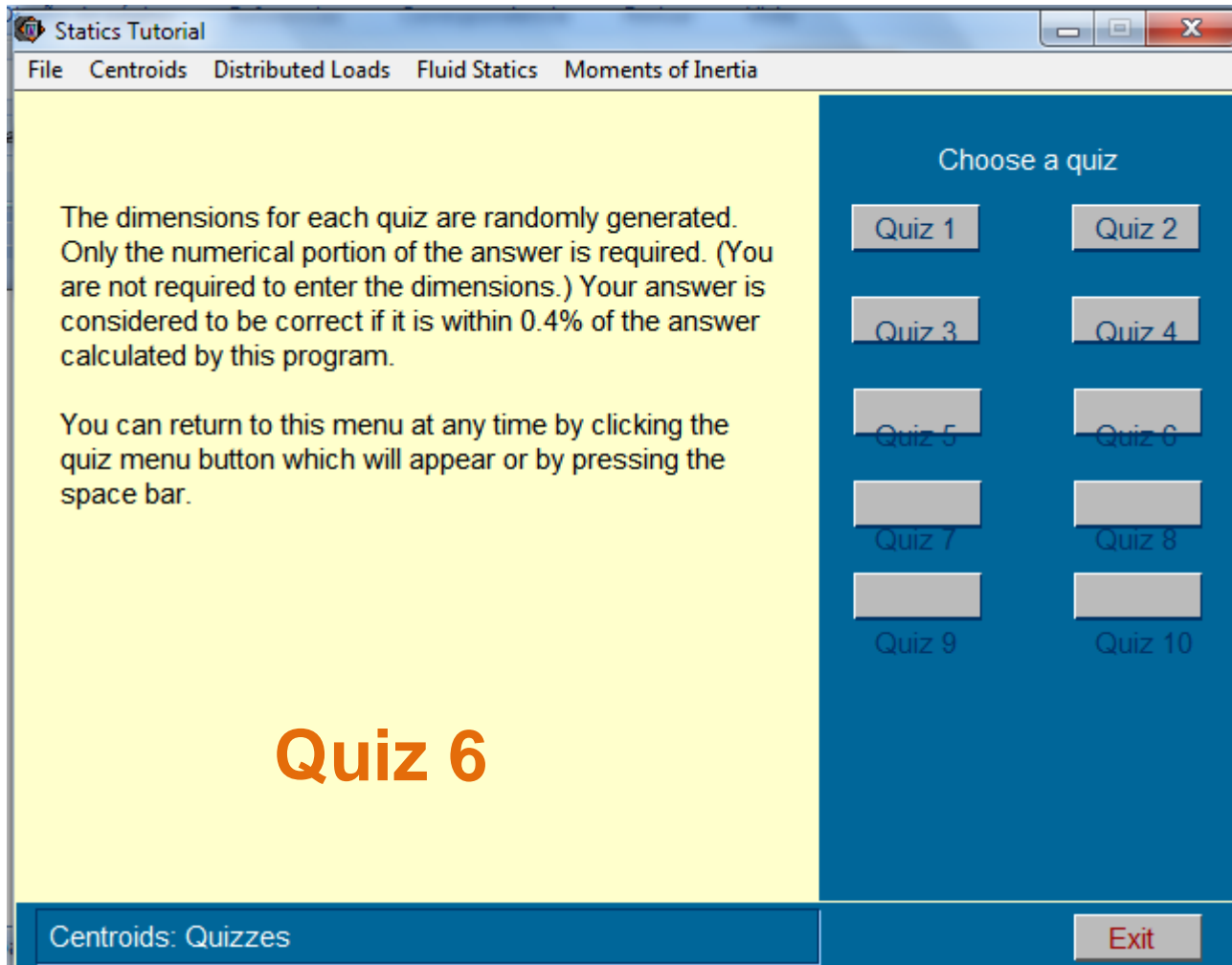
In the next section, the shear force is linear and the moment varies parabolically. The shear diagram is positive, and the moment increases. This results in the moment diagram shape shown. Finding the area under the shear diagram in this section of the beam requires computing two areas.

In the next section of the beam the shear diagram is constant; therefore the moment diagram varies linearly.

In the final section of the beam the shear force is constant, so the moment varies linearly. Since the shear force is negative, the moment decreases.







## Quiz 6

Statics Tutorial

File Shear & Moment Diagrams Friction

600 lb/ft

18 ft

6 ft

A

B

V(lb)

M (lb-ft)

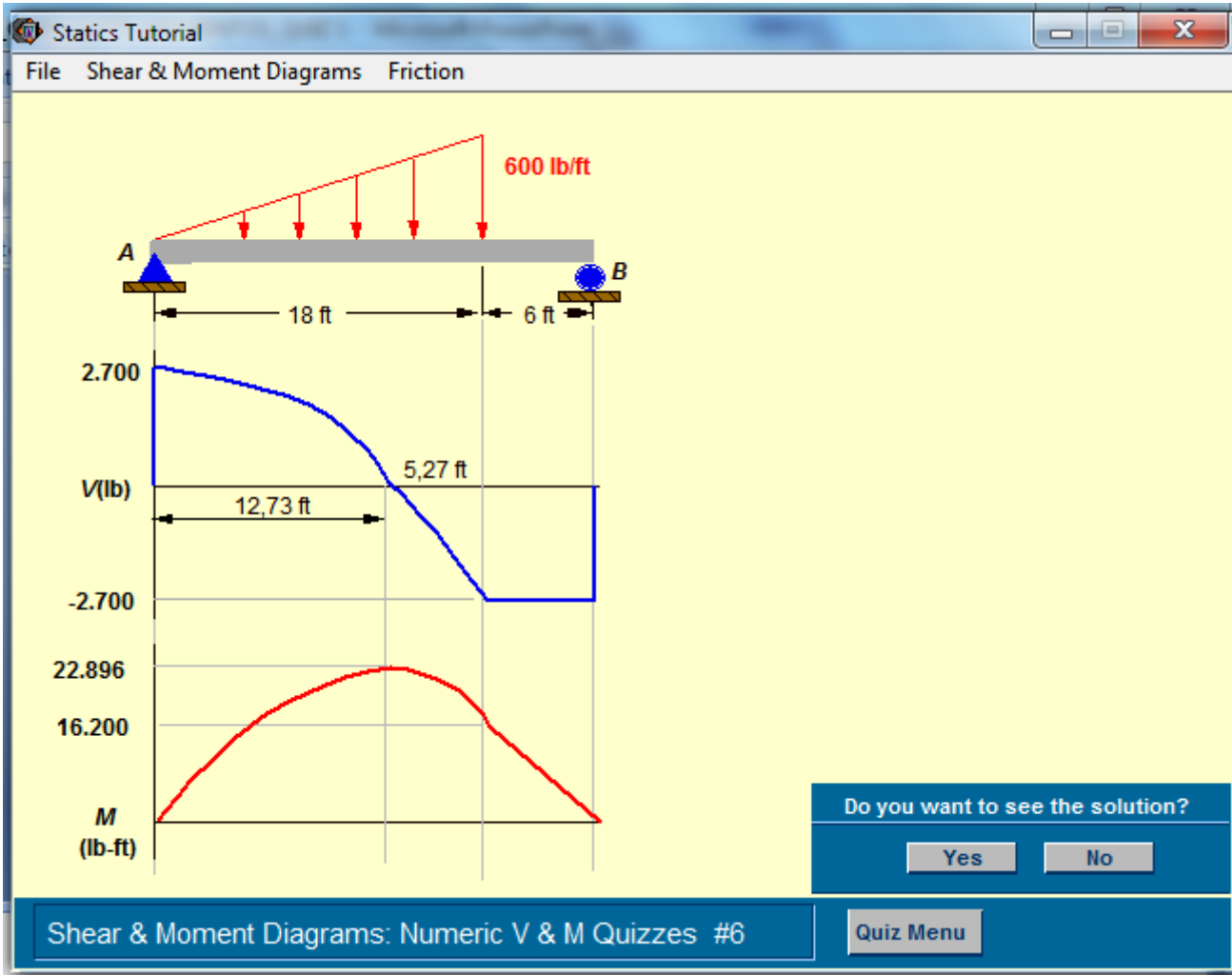
The simply supported beam shown is 24 ft long and supports a linearly varying load of 600 lb/ft over 18 ft of its span. Plot the shear and bending moment diagrams. The horizontal reaction at **A** is zero.

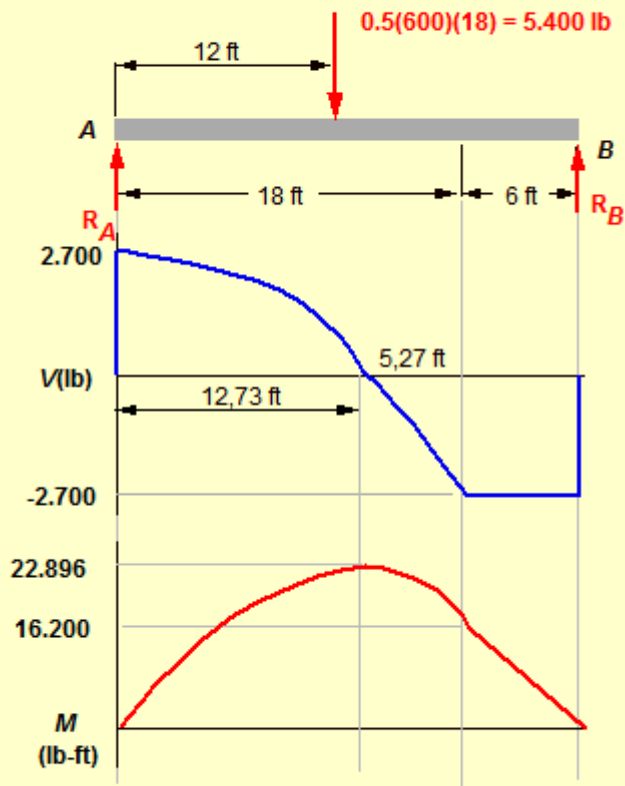
After constructing your diagram, click the box below to see the correct shear diagram.

View Diagrams

Shear & Moment Diagrams: Numeric V & M Quizzes #6

Quiz Menu





First, establish the reactions at A and B. The reactions are determined by first modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions. The equations of equilibrium are

$$+\uparrow \Sigma F_y = 0: R_A + R_B - 5,400 = 0$$

$$R_A + R_B = 5,400 \quad (1)$$

$$+\curvearrowleft \Sigma M_A = 0: 24(R_B) - 12(5,400) = 0$$

Substituting  $R_B = 2,700 \text{ lb}$  into equation (1) and solving yields  $R_A = 2,700 \text{ lb}$

Statics Tutorial

File Shear & Moment Diagrams Friction

600 lb/ft

A B

$R_A$   $R_B$

18 ft 6 ft

2.700

V (lb)

5.27 ft

12.73 ft

-2.700

22.896

16.200

M (lb-ft)

First, establish the reactions at A and B .  
 The reactions are determined by first modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions. The equations of equilibrium are

$$+\uparrow \Sigma F_y = 0: R_A + R_B - 5.400 = 0$$

$$R_A + R_B = 5.400 \quad (1)$$

$$+\curvearrowleft \Sigma M_A = 0: 24(R_B) - 12(5.400) = 0$$

Substituting  $R_B = 2.700 \text{ lb}$  into equation (1) and solving yields  $R_A = 2.700 \text{ lb}$

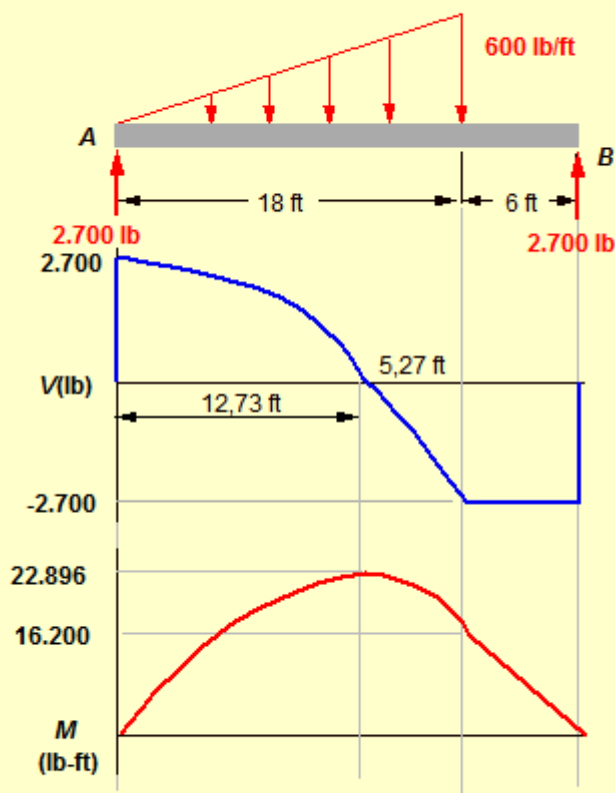
The shear diagram can be constructed once the reactions are known.

Shear & Moment Diagrams: Numeric V & M Quizzes #6

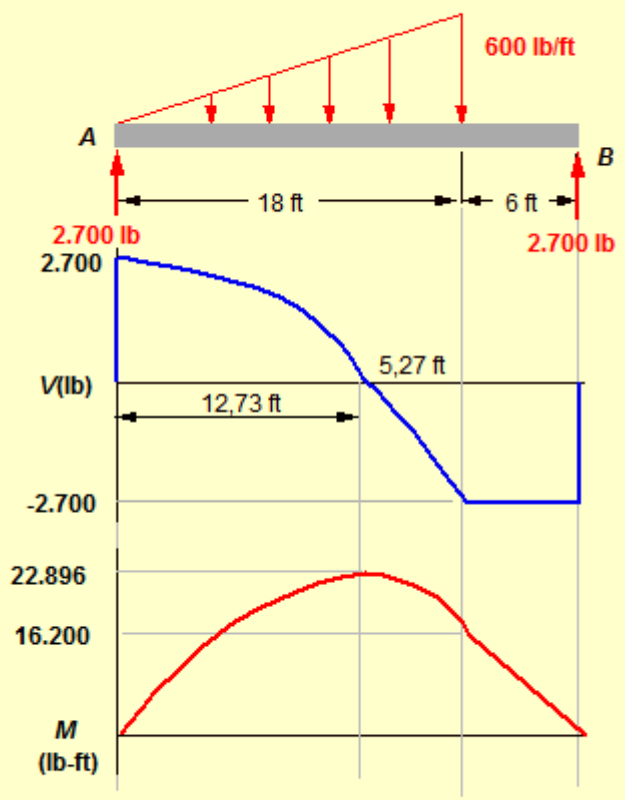
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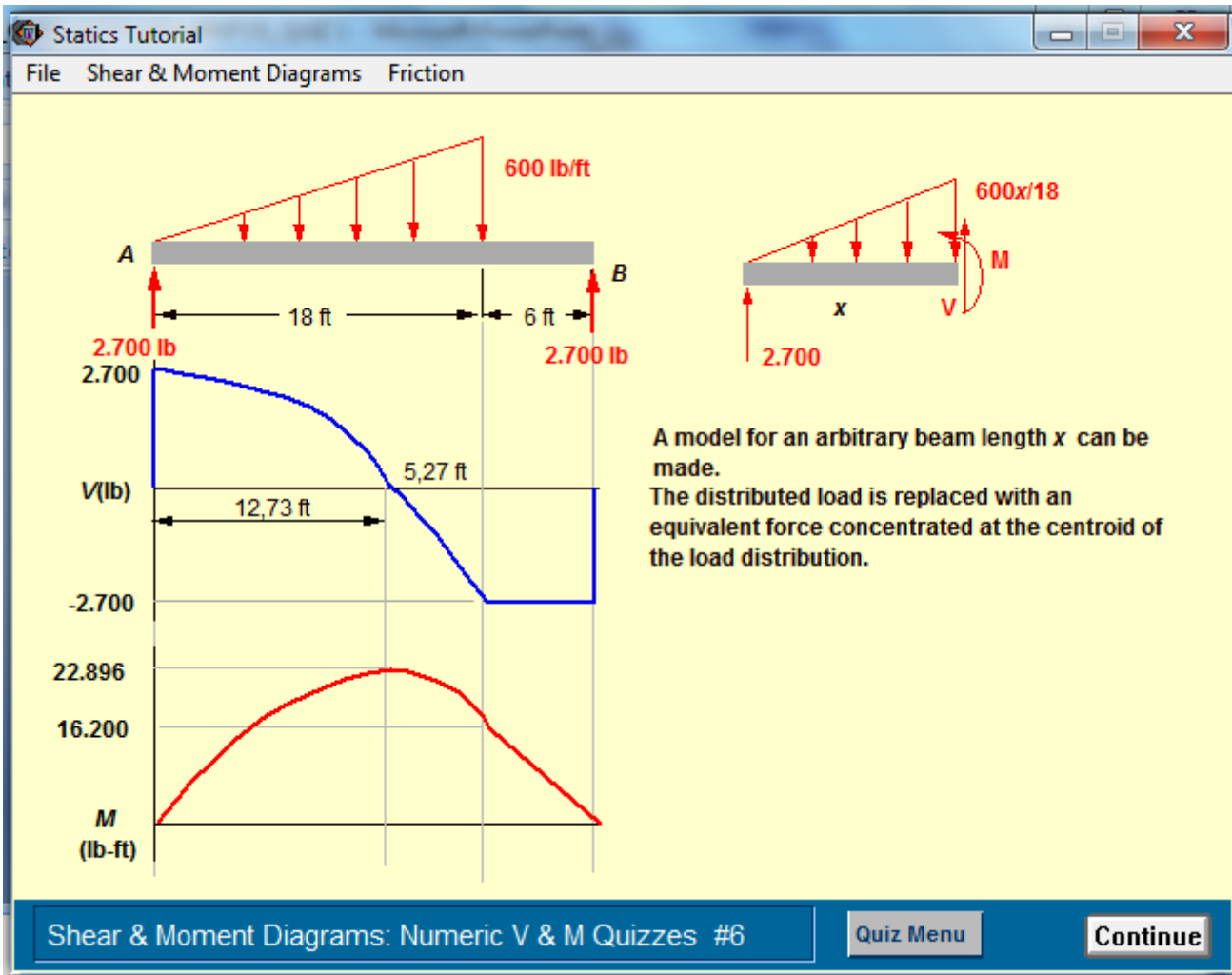


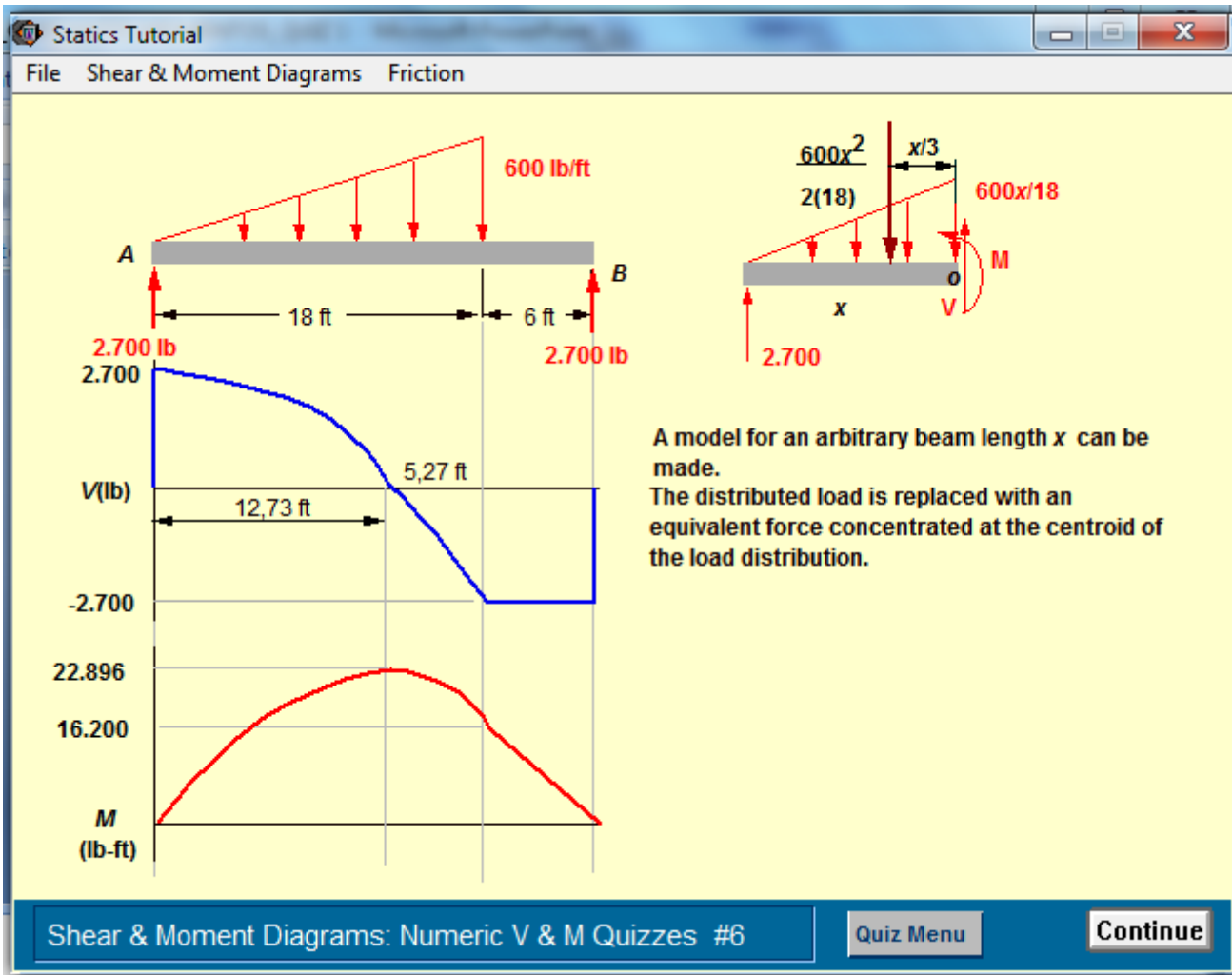
Since the load distribution is linear, it is best to construct a model and set up the equations of static equilibrium for the segment of the beam under the distributed load. Although the shear diagram can be drawn by inspection, several important features are not easily determined. For example, the point at which the shear force is zero must be determined in order to establish the maximum moment.

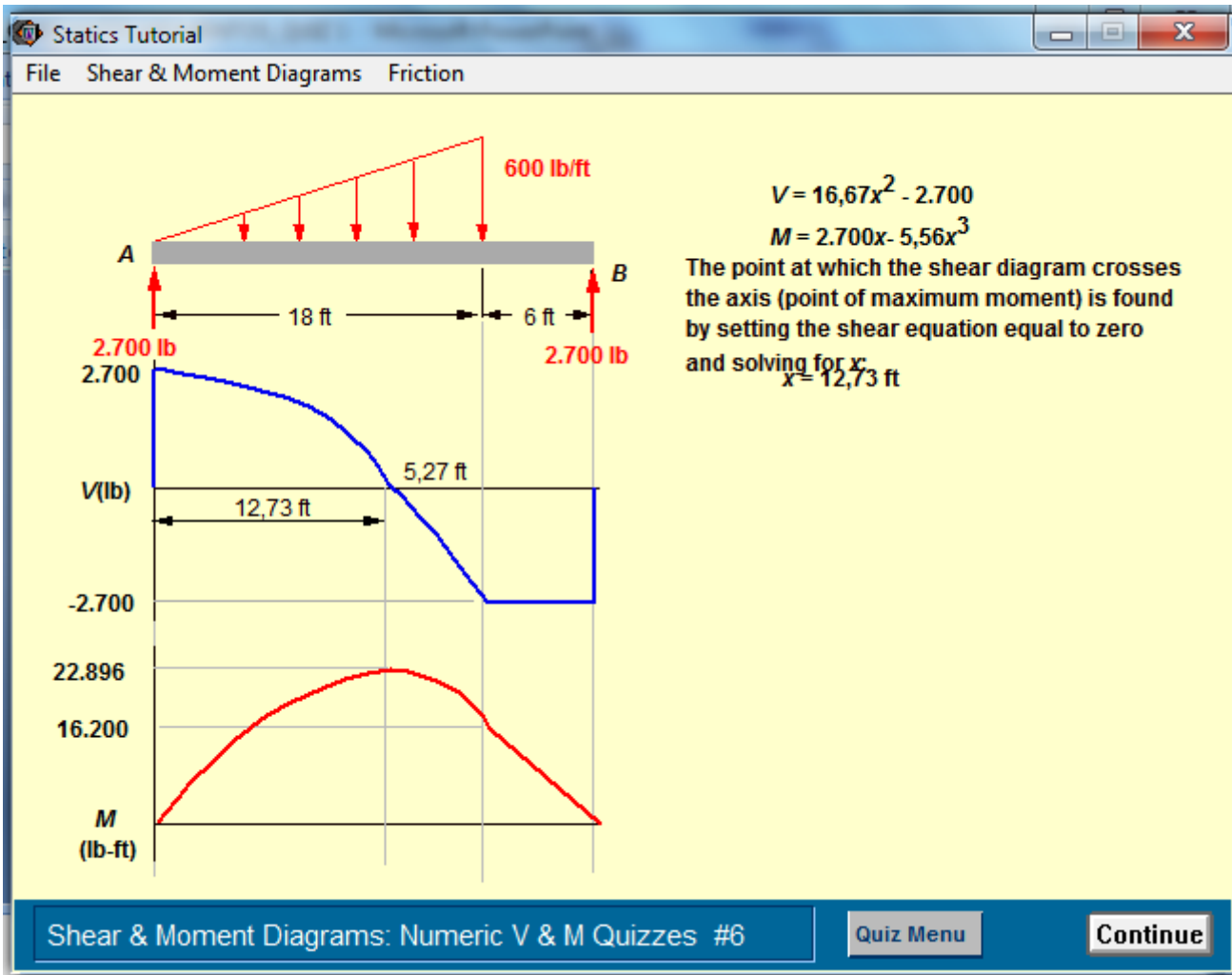


Since the load distribution is linear, it is best to construct a model and set up the equations of static equilibrium for the segment of the beam under the distributed load. Although the shear diagram can be drawn by inspection, several important features are not easily determined. For example, the point at which the shear force is zero must be determined in order to establish the maximum moment. The load must be accurately represented as a function of  $x$ . The 600-lb/ft distribution is at the right end of the load. At some arbitrary location it will be different. Since the distribution is linear, a simple equation for a line is used to define the distributed load.

$$w = 600x/18$$







Statics Tutorial

File Shear & Moment Diagrams Friction

$V = 16,67x^2 - 2,700$   
 $M = 2,700x - 5,56x^3$

The point at which the shear diagram crosses the axis (point of maximum moment) is found by setting the shear equation equal to zero and solving for  $x$ :  
 $x = 12,73 \text{ ft}$

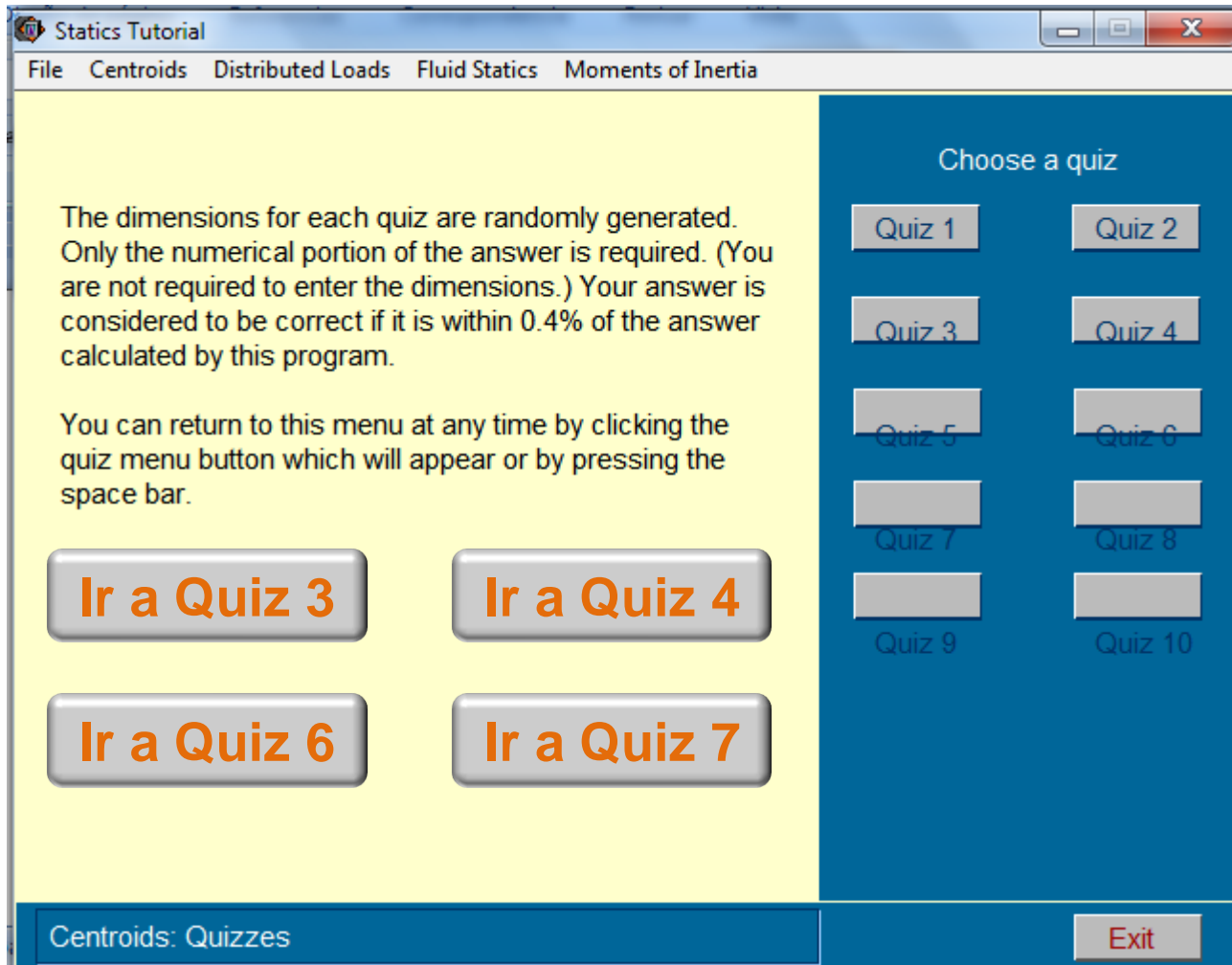
Using this value of  $x$ , and the moment equation, the bending moment at any spanwise location between  $0 < x < 18$  can be determined, using  
 $M = 2,700x - 5,56x^3$

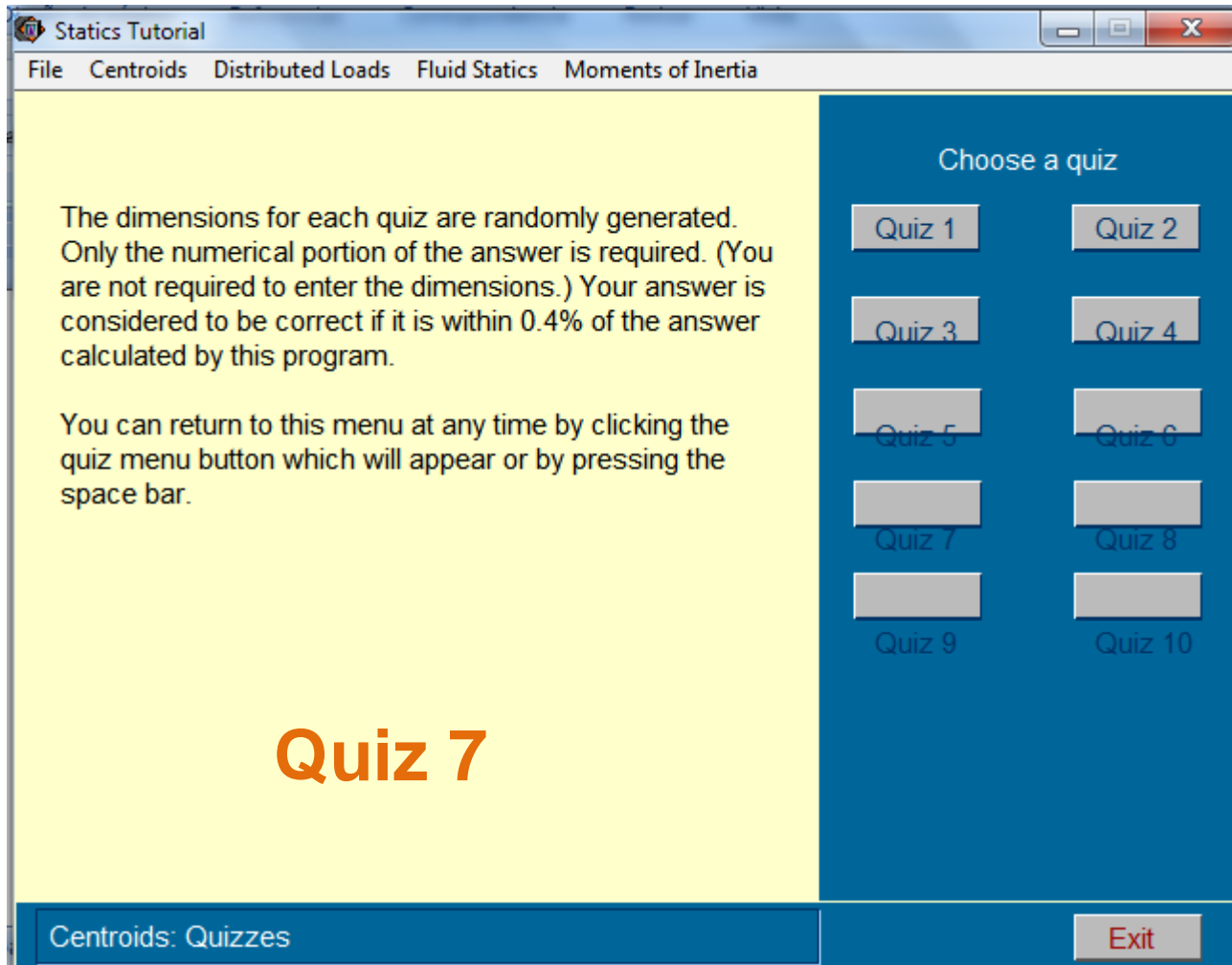
Similarly, the shear force can be determined at any point in this region using the equation for  $V$  above.

In any region of the beam outside the linearly distributed load, the method of inspection works well. In the final segment of the beam the shear force is constant until the reaction at  $B$  is reached, which brings it back to zero. The area in this segment of the shear diagram is easily computed to be  $A = 6(-2,700) = 16,200$ . When added to the moment calculated at  $x = 18$ , the result is as shown. Since the shear force is constant in this section, the moment varies linearly.

Shear & Moment Diagrams: Numeric V & M Quizzes #6

Quiz Menu Continue





## Quiz 7



Statics Tutorial

File Shear & Moment Diagrams Friction

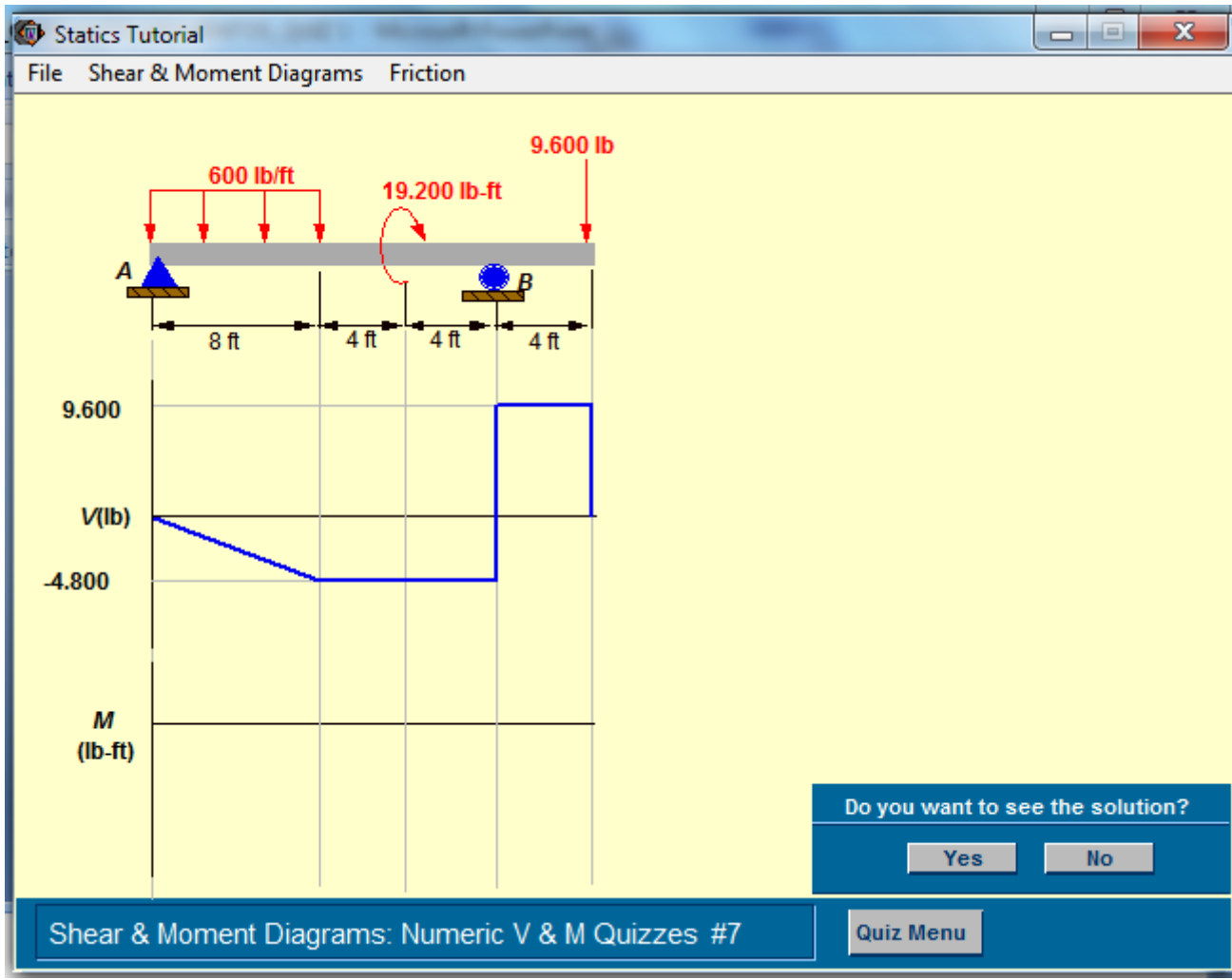
The simply supported beam shown is 20 ft long and supports a uniform load of 600 lb/ft over 8 ft of its span. A 9,600-lb concentrated load and a 19,200-lb concentrated moment are applied at the locations shown. Plot the shear and bending-moment diagrams for this beam. The horizontal reaction at **A** is zero.

After constructing your diagram, click the box below to see the correct shear diagram.

View Shear Force Diagram

Shear & Moment Diagrams: Numeric V & M Quizzes #7

Quiz Menu



Statics Tutorial

File Shear & Moment Diagrams Friction

The diagram shows a horizontal beam of total length 20 ft. At the left end (point A), there is an upward reaction force  $R_A$ . A uniformly distributed load of  $600 \text{ lb/ft}$  is applied downwards over the first 8 ft of the beam. At the midpoint of this distributed load (4 ft from the left end), there is a counter-clockwise moment of  $19,200 \text{ lb-ft}$ . At the right end (point B), there is an upward reaction force  $R_B$  and a downward point load of  $9,600 \text{ lb}$ . The beam is divided into four segments of 4 ft each by vertical grid lines.

The Shear Force Diagram (V) is shown in blue. It starts at  $R_A = 9,600 \text{ lb}$  at point A. It decreases linearly to  $-4,800 \text{ lb}$  at the 8 ft mark. It remains constant at  $-4,800 \text{ lb}$  through the 12 ft mark. At the 12 ft mark, there is a vertical jump up to  $9,600 \text{ lb}$ . It remains constant at  $9,600 \text{ lb}$  through the 16 ft mark. At the 16 ft mark, there is a vertical jump down to  $0 \text{ lb}$ . It remains at  $0 \text{ lb}$  through point B at 20 ft.

The Moment Diagram (M) is shown in blue. It starts at  $0 \text{ lb-ft}$  at point A. It increases parabolically to a maximum of  $19,200 \text{ lb-ft}$  at the 8 ft mark. It then decreases linearly to  $0 \text{ lb-ft}$  at the 12 ft mark. It remains constant at  $0 \text{ lb-ft}$  through the 16 ft mark. At the 16 ft mark, there is a vertical jump down to  $-9,600 \text{ lb-ft}$ . It remains constant at  $-9,600 \text{ lb-ft}$  through point B at 20 ft.

The first step is to establish the reactions at A and B.  
 The reactions are determined by first modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions.

Shear & Moment Diagrams: Numeric V & M Quizzes #7

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Statics Tutorial

File Shear & Moment Diagrams Friction

$600(8) = 4,800 \text{ lb}$   
 $19,200 \text{ lb-ft}$   
 $9,600 \text{ lb}$

The first step is to establish the reactions at A and B.

The reactions are determined by first modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions.

The equations of equilibrium are

$$+\uparrow \Sigma F_y = 0: R_A + R_B - 4,800 - 9,600 = 0$$

$$R_A + R_B = 14,400 \quad (1)$$

$$+\circlearrowleft \Sigma M_A = 0: 16(R_B) - 4(4,800) - 19,200 - 20(9,600) = 0$$

$$R_B = 14,400 \text{ lb}$$

Substituting 14,400 lb into equation (1) and solving yields

$$R_A = 0 \text{ lb}$$

Shear & Moment Diagrams: Numeric V & M Quizzes #7

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Statics Tutorial

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The first step is to establish the reactions at A and B.

The reactions are determined by first modeling the distributed load as an equivalent concentrated force, then generating the equations which satisfy the equilibrium conditions.

The equations of equilibrium are

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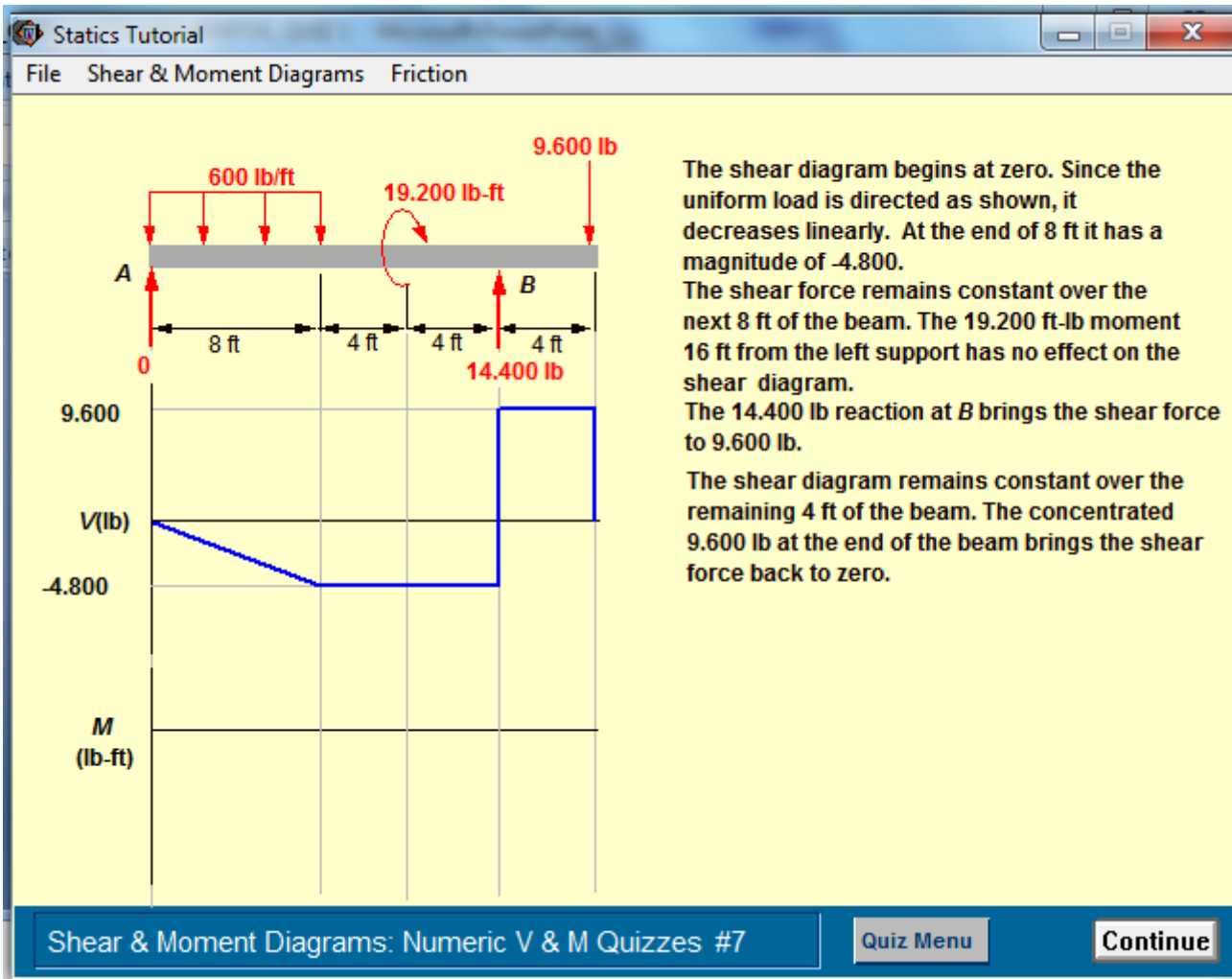
$$R_A = 0 \text{ lb}$$

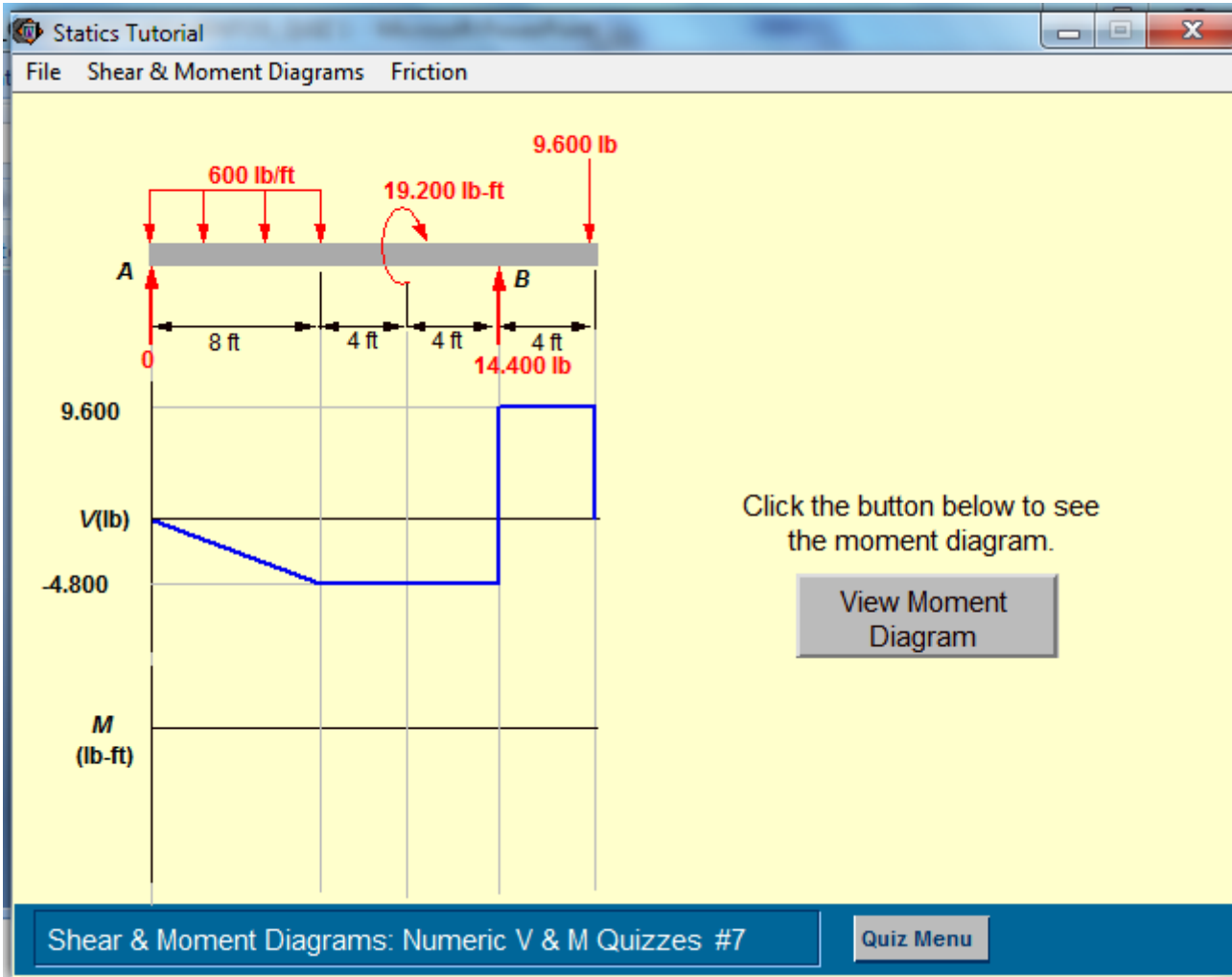
The shear diagram can be constructed once the reactions are known.

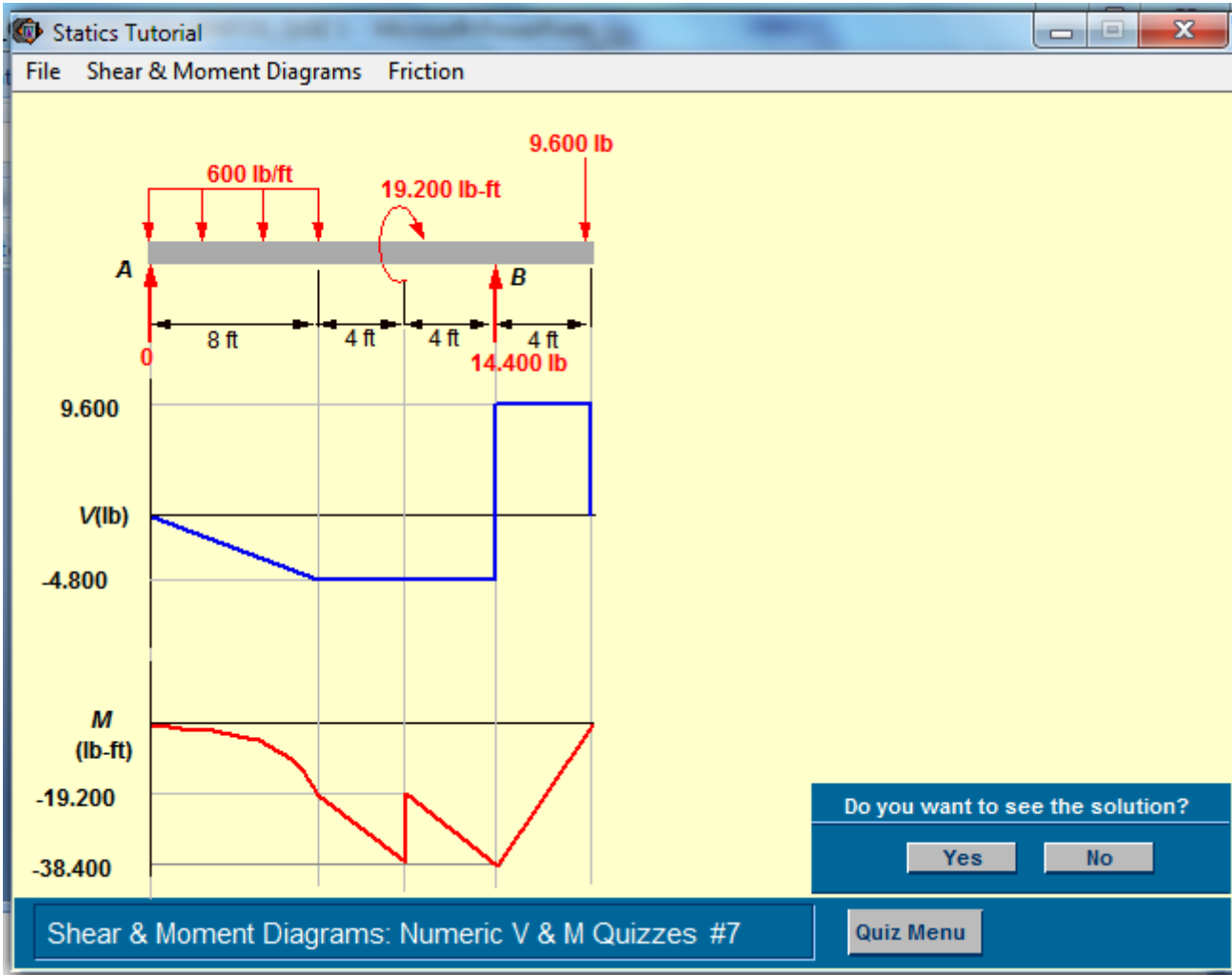
Shear & Moment Diagrams: Numeric V & M Quizzes #7

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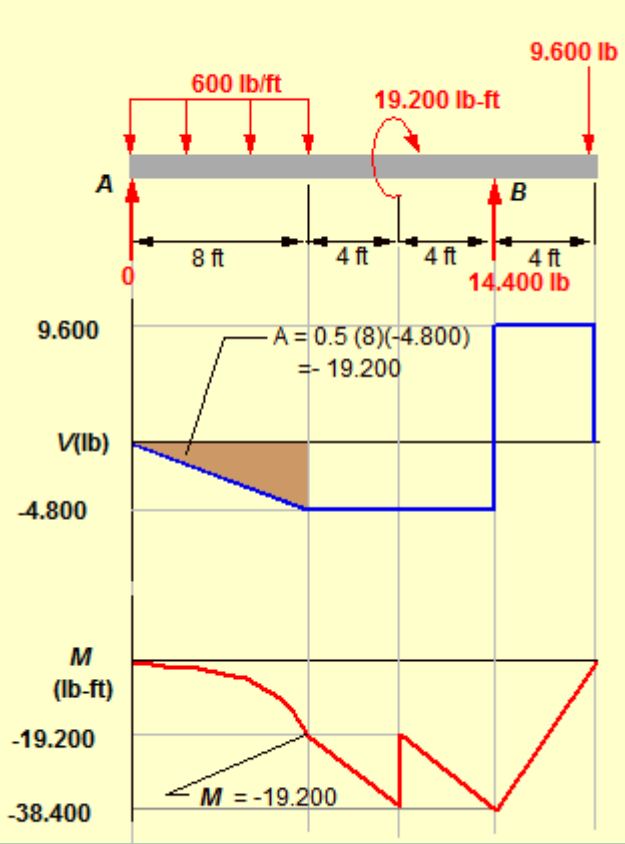
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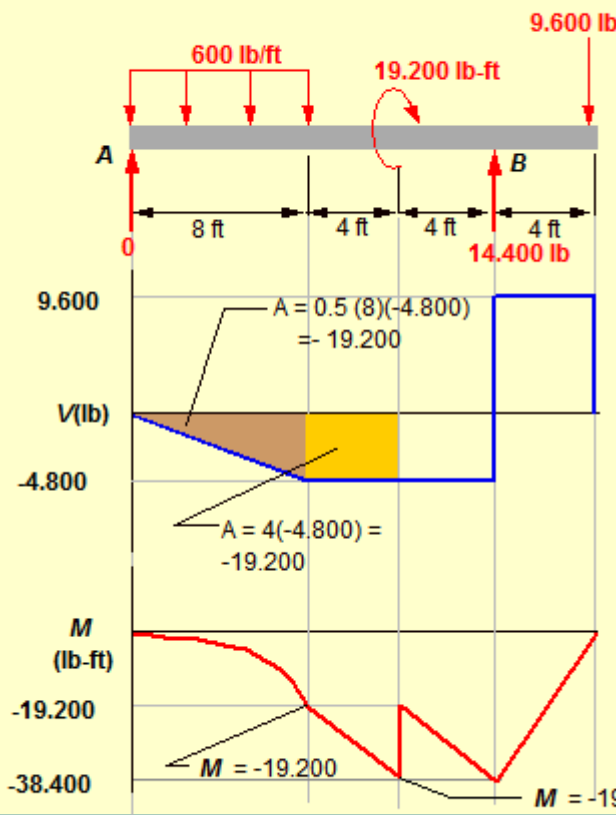




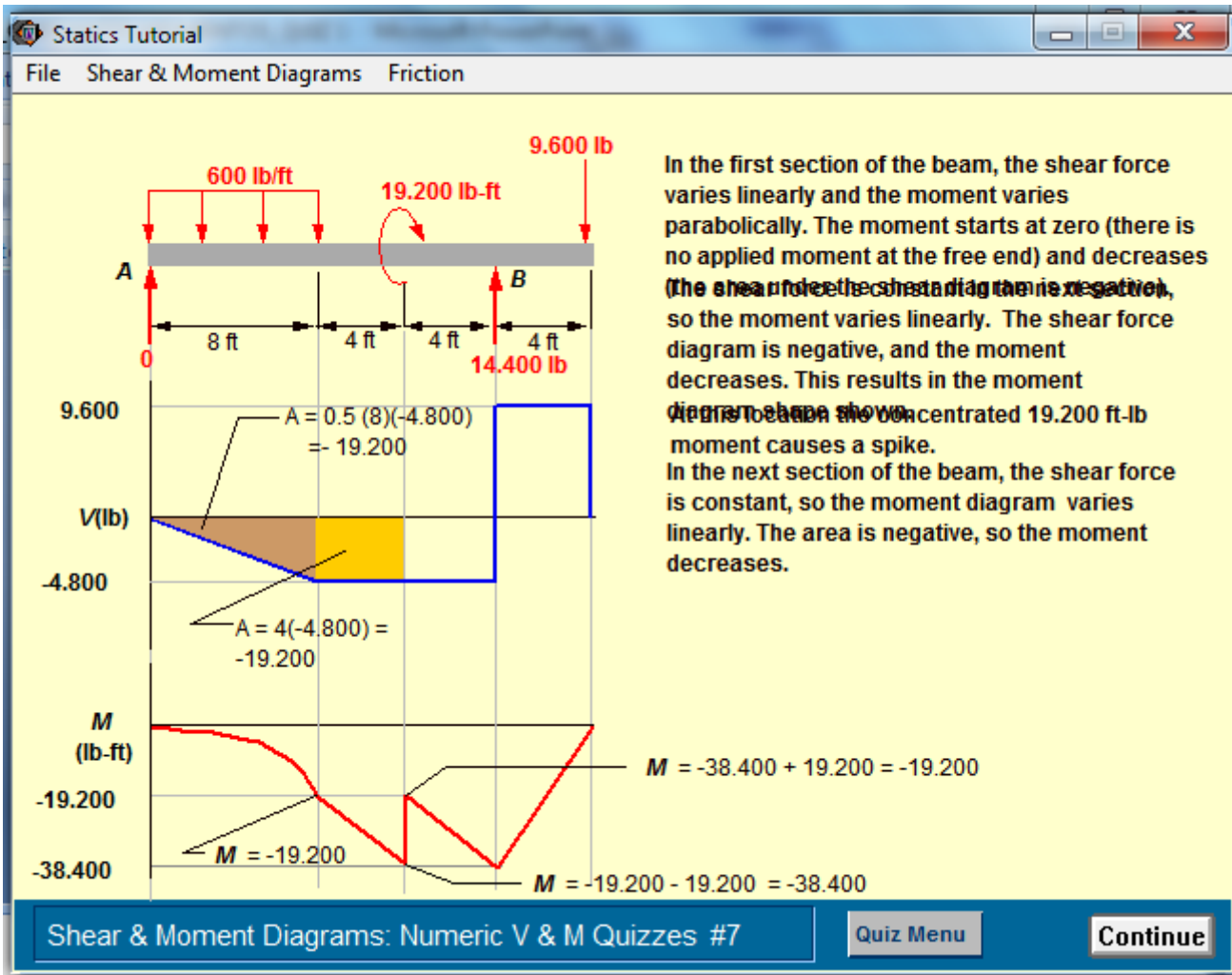


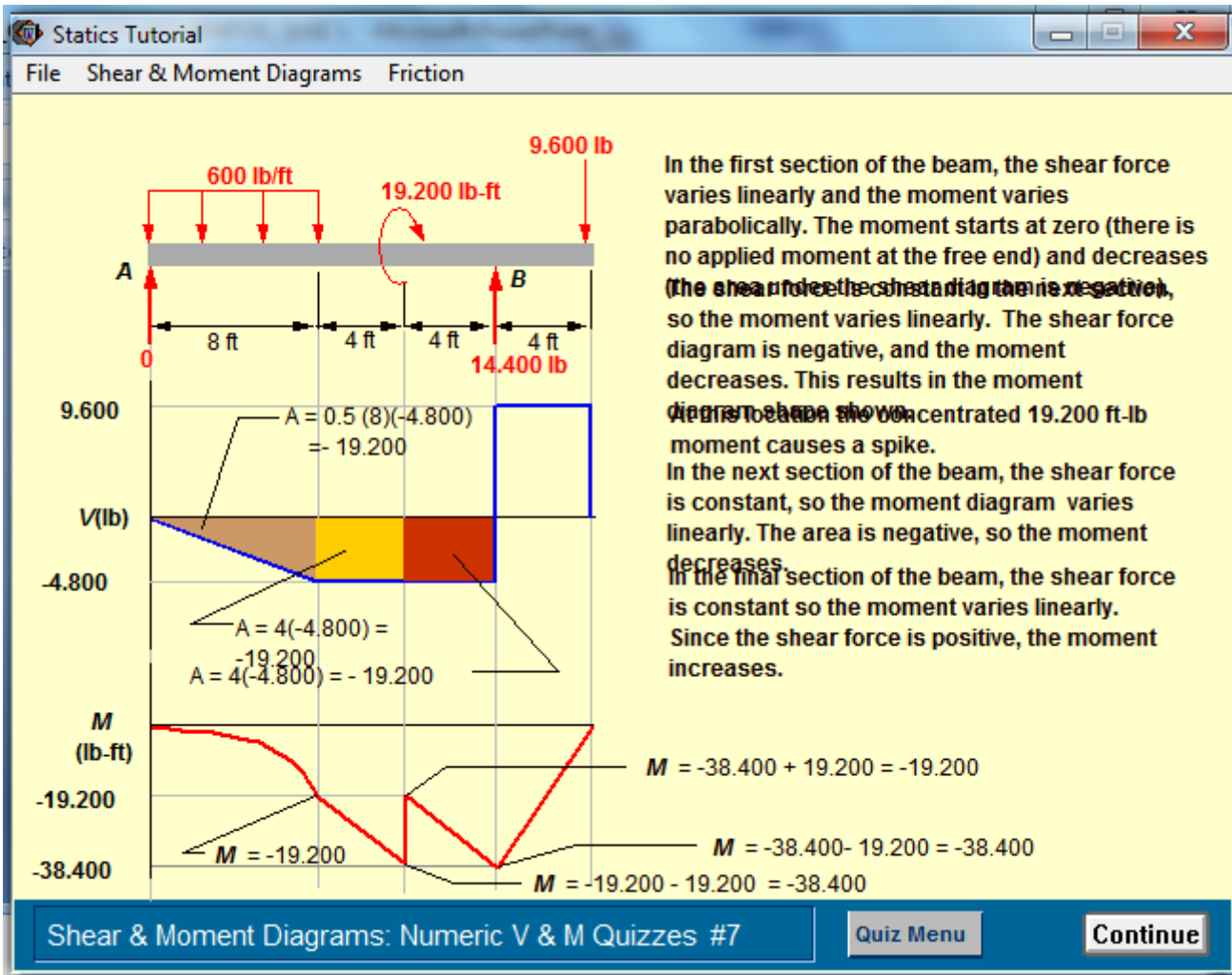


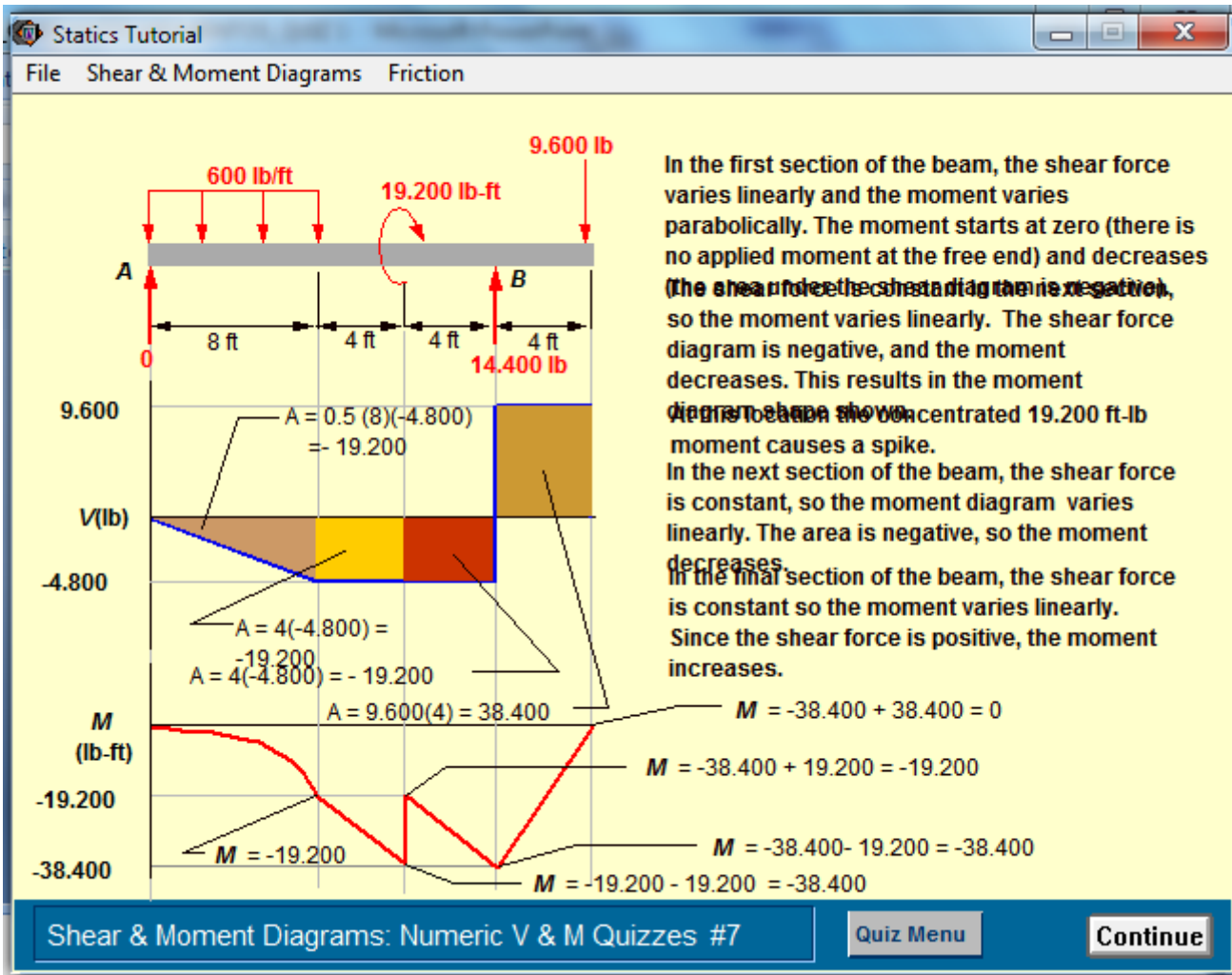
In the first section of the beam, the shear force varies linearly and the moment varies parabolically. The moment starts at zero (there is no applied moment at the free end) and decreases (the shear force for the shear diagram is negative), so the moment varies linearly. The shear force diagram is negative, and the moment diagram shape shown.



In the first section of the beam, the shear force varies linearly and the moment varies parabolically. The moment starts at zero (there is no applied moment at the free end) and decreases (the shear force in the shear diagram is negative), so the moment varies linearly. The shear force diagram is negative, and the moment decreases. This results in the moment diagram shape shown.







**SHEAR & MOMENT DIAGRAMS.  
QUIZZES  
VIGA SIMPLEMENTE APOYADA  
(QUIZ 3 – 4 – 6 – 7)**

Los ejercicios siguientes se realizan con el **SOFTWARE STATICS**, incluido en “MECÁNICA VECTORIAL PARA INGENIEROS. ESTÁTICA”. Sexta edición. MCGRAW-HILL. 1997 ISBN 84-481-1079-X.

La presentación se realiza exclusivamente con fines educativos, para facilitar su discusión en clase.